

ELECTRICAL AND ELECTROMAGNETIC BOREHOLE MEASUREMENTS: A REVIEW

B. R. SPIES

Schlumberger-Doll Research, Old Quarry Road, Ridgefield, Connecticut 06877-4108, USA

Abstract. Electrical and electromagnetic geophysical techniques have reached a high level of technological sophistication since they were first used in boreholes less than one hundred years ago. Borehole logging – the detailed determination of rock and fluid properties adjacent to the borehole, and borehole geophysics – extending the range of geophysical investigation large distances away from the borehole, are essential for exploration, assessment and production of earth resources, as well as for fundamental studies of the earth. Borehole electrical and electromagnetic methods incorporate 17 decades of the electromagnetic spectrum, from 1000-s geomagnetic studies, through resistivity and permittivity measurements, to high-resolution resistivity imaging, NMR and optical spectroscopy.

Key words: Borehole, Logging, Resistivity, Electrical, Electromagnetic, Spontaneous Potential, Radar, Tomography, History

1. Introduction

The use of electrical and electromagnetic (EM) techniques for studying the earth dates back to eighteenth century measurements of the electrical conductivity of mineral samples and the earth, and the observation of fluctuating earth currents in long grounded wires. The methods were improved over the ensuing two hundred years, and by the early 1900s were being used in many countries for mineral exploration. The first underground measurements were made in mines in the late 1800s, but it was not until 1913 that electrodes were first lowered down boreholes.

In the intervening 82 years borehole techniques have risen to a high level of sophistication, and are now applied in fields as varied as mineral and petroleum exploration, geotechnical and environmental investigations and fundamental studies of stress and petrophysics in deep crustal boreholes. Present technology ranges from inexpensive resistivity probes used for shallow boreholes, to advanced at-the-bit resistivity tools used to guide 8-km long horizontal wells along narrow stratigraphic intervals to efficiently drain petroleum deposits.

This paper gives a brief overview of borehole electrical and EM borehole methods as applied in these diverse fields, and attempts to cover the broad range of applications and techniques in use today. By necessity the coverage will not be complete, but key references will be given to other review papers and bibliographies compiled in specific fields of study. The review focusses on English language literature, and does not attempt to cover papers published in other languages, although some key results are mentioned. Historical developments are drawn from

Kelly (1950), Johnson (1962), Kunez (1966), van Nostrand and Cook (1966), Segesman (1980), and Ward (1980).

1.1. THE FOUNDATIONS OF SURFACE ELECTRICAL AND ELECTROMAGNETIC METHODS

The earliest studies of electrical prospecting, according to Jakosky, (1940), can be traced back to 1720, when Stephen Gray and Granville Wheler tabulated the electrical conductivities of rocks, and 1746 when William Watson discovered independently that the ground is an electrical conductor.

It was later recognized that naturally occurring potentials exist in the vicinity of metalliferous ore deposits, and a number of workers attempted to exploit this new art of ore-finding. The first systematic studies of natural electrical potentials are usually credited to Robert W. Fox in England, who published a series of papers starting with Fox (1830) on the electrical potentials generated by sulphide deposits in Cornwall. The United States Geological Survey (USGS) carried out a major series of field studies in 1880 of the natural earth potentials in the Comstock gold lode in Nevada (Barus, 1882). Interestingly, Barus is often credited with developing the first non-polarising electrode, although non-polarizing electrodes were employed by Matteucci (see below) forty years earlier. In 1894 P. Bachmetjew in Germany identified a potential attributed to the movement of groundwater through subsurface sands. He based the explanation of these potentials on streaming potential or electrokinetic effects discovered by G. Quinke in 1859 and later studied by Helmholtz in 1879 (Rust, 1938). Further contributions at the USGS (Wells, 1913; Wells, 1914) developed the electrochemical basis of the passive self-potential phenomena.

Watson, in his 1746 work referred to above, also noted that the current passed through the ground between electrodes spaced 3 km apart varied in an erratic manner, different than if wire were used instead. The fluctuations were, of course, caused by telluric currents. Fox in the 1830s had also noted fluctuations in his earth currents measurements at Cornwall, which he attributed to opposing energies of currents in metalliferous deposits and interactions with earthquakes and volcanic activity. The first serious attempt to understand these fluctuations was by Charles Matteucci of the Greenwich Observatory, who in 1847 observed that earth currents in telegraph wires correlated with the aurora borealis (Matteucci, 1865). Further fundamental studies relating the earth's natural currents and magnetism followed in the early 20th century (van Bemmelen, 1908; Gish, 1923; Mauchly, 1918).

In the late nineteenth century various patents were granted in Britain and the USA for prospecting methods using direct or alternating currents at low frequencies to measure differences in the earth's electrical properties associated with ore deposits. The earliest techniques measured the resistance of the ground between two electrodes (e.g., Fred H. Brown between 1883 and 1891) but were strongly affected by the region near the electrodes. Leo Daft in 1897, and Daft and Alfred

Williams in 1902 used alternating currents and mapped equipotentials with telephone receivers connected to two search electrodes placed on the ground. This technique suffered from inductive coupling between the transmitter and receiver wires (van Nostrand and Cook, 1966). The Daft-Williams method was also used in Sweden in 1906, with an alternating current of 10 to 40 mA and a voltage of 5,000 to 60,000 volts. An important advance in resistivity measurements was the development of a four-electrode resistivity array by Frank Wenner of the U.S. Bureau of Standards (Wenner, 1912, 1915). Wenner also described a normalization procedure to convert the measured data to "effective resistivity".

In France in 1912, Conrad Schlumberger improved the two-electrode resistance method by mapping equipotentials around a source electrode energized by d.c.. Schlumberger first plotted the electrical potentials at his family estate in Normandy, followed by another test at Sassy and a third in 1913 at Fierville-la-Campagne in the Calvados iron-ore basin (Allaud and Martin, 1977). Conrad tested the use of a short electrical dipole to attain greater precision, and identified anisotropy effects in the dipping strata. He also noted that switching transients were higher near buried steel pipes, and identified these effects as "polarization provoquée" (induced polarization), which he further developed in 1913. Independently, in the USA, (McCollum and Logan, 1913) studied "self corrosion" effects between metal pipes and the earth and polarization effects in soils.

Also in 1913, at Bor, Servia, Conrad Schlumberger found that if a transmitting electrode were implanted in an orebody, then the whole orebody was raised to the same potential and the orebody could be outlined by plotting equipotentials. This method, which Schlumberger called the "grounding method", later became known as *mise-à-la-masse*. In 1919 the younger brother Marcel joined Conrad Schlumberger to form a commercial venture to explore for metallic ores and conduct geophysical surveys, and from 1920 made use of the four-electrode technique and an apparent resistivity formulation. A summary of these early experiments is given by Schlumberger (1920) and Allaud, *et al.*, (1977).

Inductive electromagnetic (EM) methods were developed after galvanic methods were well established. In 1910-1911 the Germans Lowry and Leimbach experimented with EM at radio-frequency EM prospecting. In 1925 Harry W. Conklin received a patent for mining exploration with an high-frequency EM method (Conklin, 1917). Conklin used a surface transmitter coil 60 m in diameter and measured positions of equal intensity ("isogonal lines") using two receiver coils connected in opposition. Rapid development of EM for prospecting was made in Sweden from 1921 with the Sundberg EM method (Sunberg, *et al.*, 1923; Sundberg and Hedstrom, 1934), the forerunner of the highly successful horizontal-loop or slingram EM method.

1.2. THE EMERGENCE OF BOREHOLE LOGGING

Rust (1938) reports that in 1913 a borehole resistance log was made in Germany by Richard Ambronn, who placed one electrode at the surface and lowered the other through the drilling fluid down a borehole. The first quantitative borehole resistivity measurement is usually attributed to Marcel Schlumberger in 1921. Marcel determined in situ the resistivity of sediments in the Bessegès coal basin to help interpret a surface equipotential survey by lowering electrodes to the bottom of a 750-m hole. The next borehole measurement was not made until 1927, in the Pechelbronn oil field in eastern France (Figure 1), by Henri Doll who had joined the Schlumberger brothers and directed their research at oil wells, where a much larger commercial market existed. From 1927 onwards rapid progress was made in borehole electrical techniques, based largely on experience with surface-based measurements.

The Schlumbergers called their borehole method “electrical coring” in analogy with the geologic coring (in 1933 the name of the technique changed to electrical logging). In 1927 the 3-electrode lateral array (one current electrode and two potential electrodes downhole) was developed, as was the concept of guard electrodes (called the current output sonde) to focus current into the formation and to reduce borehole effects. Also in 1927 the dip of the strata crossing the borehole was measured by detecting the distortion of equipotentials around the current electrode. In 1932 an inductive compass for dip measurements called the “electromagnetic inclinometer” was commercialized. Schlumberger obtained a French patent in 1928 on the use of the S.P. curve to locate permeable strata, after noting that field measurements of the naturally-occurring potential showed large excursions above and below oil sands. The effect was shown to be unrelated to electrode polarization, and was attributed to filtration of drilling mud into the formation (Schlumberger *et al.*, 1932). It was soon realised (Schlumberger *et al.*, 1933) that SP also had a large electrochemical component.

Further developments in borehole logging, extensively used in petroleum exploration and lesser in mining and geotechnical areas, are described in a later section. We will use the term “logging” for techniques where source and receiver are lowered down the same borehole, usually in a self-contained housing known as a sonde. The fundamental purpose of logging is to characterize the geological formation in the immediate vicinity of the borehole, often as a substitute for core or fluid samples. Electrical and EM logging techniques range from self-potential, through galvanic and inductive resistivity methods, to high-resolution borehole imaging techniques, to high-frequency dielectric and nuclear magnetic resonance methods.

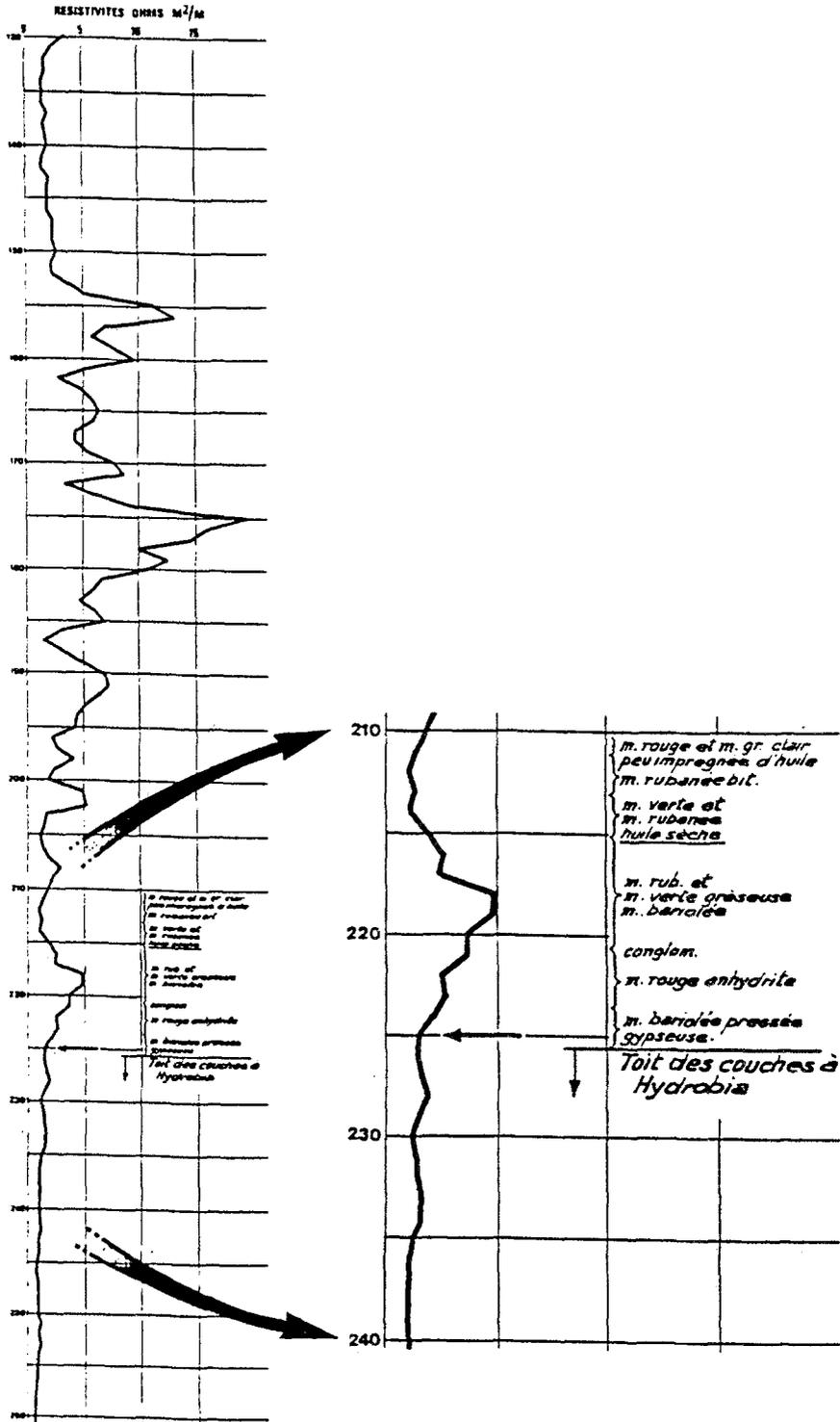


Figure 1. An early "electrical coring" made by Henri Doll in Pechelbronn, Alsace, in 1927 (Allaud and Martin, 1977).

1.3. BOREHOLE GEOPHYSICS

Borehole geophysics, in contrast to logging, attempts to probe a considerable distance away from the borehole. Borehole electrical and EM methods have become well established in the mining industry, and include *mise-à-la-masse*, borehole EM with a surface source, cross-well resistivity and cross-well EM and radar.

In the following sections we will categorize the different borehole electrical and EM methods first by frequency, and then by application. The discussion will jump from the earliest recorded use of a method directly to the present state-of-the-art. Finally, we will review how these methods are adapted for scientific studies in deep crustal boreholes.

2. Classification by Frequency

The purpose of all borehole geophysical methods is to determine, as accurately as possible, the physical properties of the subsurface geology surrounding the borehole. Electrical and EM methods are used to determine resistivity (real, complex, or anisotropic), magnetic and dielectric properties, porosity, fluid content, lithology and fracture patterns. A vast array of tools and techniques have been developed during the last 100 years to make these measurements. The design of the tool, the mode of operation, the physics of measurement, the frequency of operation, signal and noise levels are all interdependent.

Borehole electrical and EM methods cover 17 decades of frequency, from 1000-s geomagnetic measurements for crustal studies, to 1-GHz dielectric and 100 THz optical spectroscopic logging tools used in the oil industry (Figure 2). At the low end of the spectrum are measurements such as SP, d.c. resistivity and magnetometric resistivity, whose lower frequency is bounded by the instrumental switching or observation time, typically a few seconds. Logging tools, which are moved continually in a borehole as data are collected, are limited at the lower frequencies by logging speed. Galvanic resistivity logging tools, which include borehole imaging, operate in the range tens to hundreds of hertz. The frequency range of the other logging tools is determined by the physics of the measurement and practical considerations: induction conductivity devices operate at frequencies from 200 Hz to 40 kHz, whereas dielectric tools range from 20 MHz to 1 GHz. Newly developed optical spectroscopy tools for fluid identification operate in the visible region around 10^{14} Hz.

The frequencies used in borehole mineral exploration depend strongly on the resistivity of the host rock and the distance between source, receiver and target. At or near d.c. are the d.c. resistivity and IP methods, including cross-well resistivity and IP tomography. Surface-to-borehole techniques use frequencies from 10 Hz to 10 kHz. The spectrum of cross-borehole EM measurements is constrained by the skin depth: frequencies as low as 500 Hz are required in conductive formations

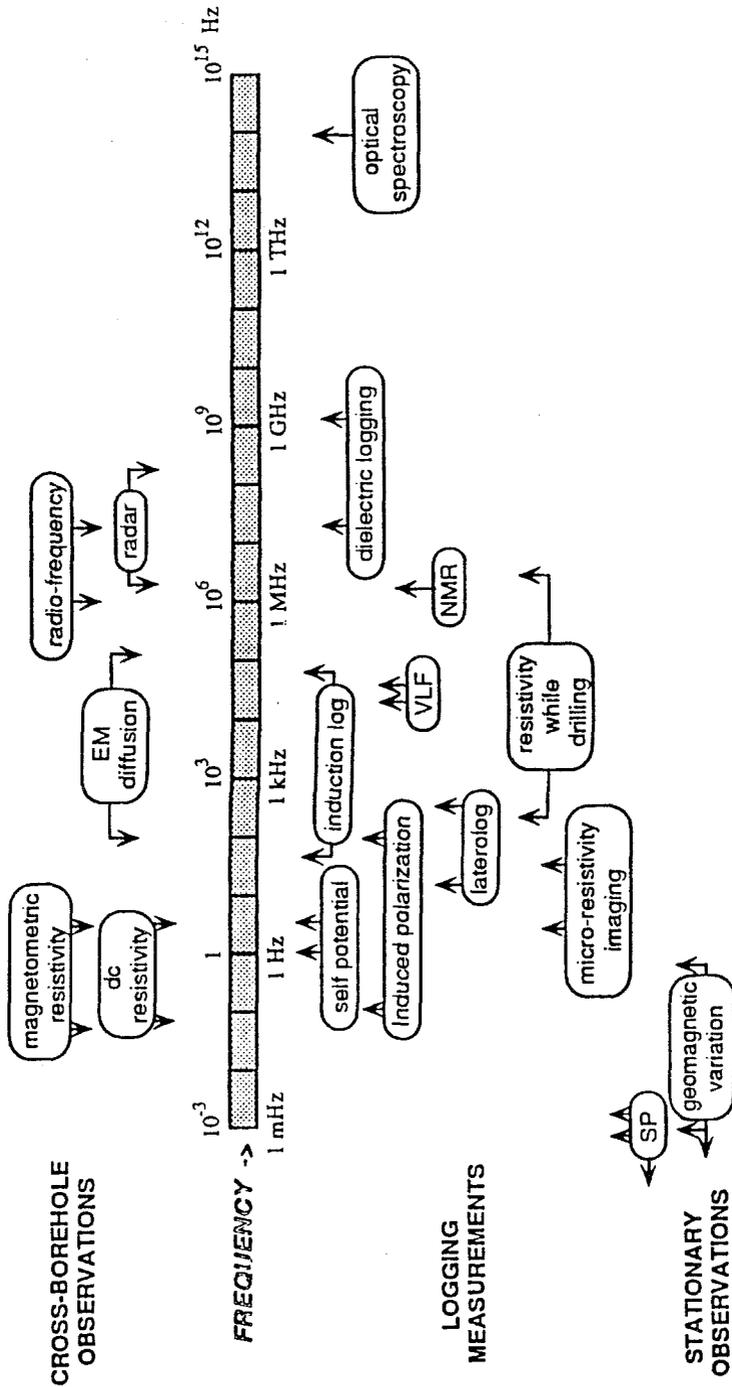


Figure 2. Spectrum of electromagnetic borehole techniques. The frequency of operation is determined by a combination of physics and practical considerations (see text).

(~ 1 S/m), radio-frequency and radar at frequencies up to 120 MHz are possible in highly resistive rocks ($> 1,000$ ohm-m).

3. Borehole Methods in Mineral Exploration

The earliest use of subsurface electrical measurements was in underground mines and workings, where geophysical equipment was taken into the mine to map extensions and hidden sections of ore. A natural development was to deploy electrodes pushed into boreholes and connected by wires to equipment in the mine or at the surface. Most of the techniques in use today bear a very close resemblance to the early methods; the major advances have come in miniaturization and improved reliability of electronics, and of course, modeling and interpretation. Excellent reviews of borehole electrical and EM methods applied to mineral exploration are given by Daniels and Dyck (1984), Dyck and Young (1985), Dyck and Asten (1988), Dyck (1975, 1991), as well as standard texts such as Grant and West (1965) and Keller (1966). Papers specialized in borehole geophysics in the minerals, geotechnical and groundwater industries are contained in the proceedings of a series of conferences (Killeen, 1985; MGLS, 1987, 1989, 1991, 1993).

3.1. GALVANIC METHODS

Galvanic methods inject d.c. or low-frequency current directly into the rock and measure potentials or potential differences. Many possibilities for electrode arrays exist, including single-borehole, borehole-to-borehole, and surface-to-borehole or borehole-to-surface. The simplest methods are self-potential (SP) and d.c. resistivity, followed by induced polarization (IP) and magnetometric resistivity (MMR). Some work on nonlinear effects at high current densities has also been done.

Borehole resistivity applications in mineral exploration and development are described in Ogilvy (1983, 1985b) and Daniels (1977, 1978, 1983). More recently, developments in borehole resistivity have focused on tomographic techniques, which are discussed later in this paper.

Induced polarization has always played an important role in mineral exploration, because of its high sensitivity to metallic minerals. The theoretic basis of IP is well summarized in the works of Wait (1959, 1989) and Madden and Cantwell (1967). The primary mechanism for IP in mineral applications is electrode polarization effects at the boundaries of electrolyte and conducting mineral grains. Borehole IP measurements have successfully been applied in mineral exploration by Wagg and Seigel (1963), Bacon (1965), Brant (1966), Mathisrud and Sumner (1967), Sumner (1976), Glenn and Nelson (1979) and more recently Ogilvy (1985a,b) and Poirmeur (1987).

In the *mise-à-la-masse* or applied potential method, current is injected directly into conductive ore intersected in the borehole, and the potential mapped either

on the surface (Jakosky, 1933; McMurray and Hoagland, 1956; Edwards, 1988; Edwards and Howell, 1976; Tyne, 1980; Witherly, 1980; Mwenifumbo, 1986; Asten, 1991) or in another borehole (Parasnis, 1967; Nabighian *et al.*, 1984; Lo and Edwards, 1986; Mwenifumbo, 1987; Ushijima, 1989; Reed, 1993).

A reciprocal geometry to *mise-à-la-masse* is to map the potential distribution in a borehole from a surface electric source. Shima (1992; 1993) use the term “vertical electrical imaging” for such an array to map the resistivity distribution away from the borehole. Cross-borehole MMR is described by Nabighian *et al.* (1984) and Mwenifumbo (1987).

3.1.1. Resistivity Tomography

The foundations of resistivity tomography were laid in the 1970s both for geophysical (Stefanescu, 1970) and medical applications, where it is also known as electrical impedance computed tomography (Lytle and Dines, 1978; Henderson and Webster, 1978; Price, 1979; Henderson and Brown, 1984; Brown *et al.*, 1985; Dijkstra *et al.*, 1993).

Resistivity tomography between boreholes requires the collection of a large matrix of d.c. electrical measurements from electrodes in both boreholes, and inversion of the data to form a resistivity image of the interborehole region. The data can also be collected between the surface and boreholes, or between subsurface engineering or mining tunnels. Geophysical applications of d.c. resistivity tomography include Daily and Yorkey (1988), Daily *et al.* (1992), Shima (1992a), Shima and Saito (1988), Shima and Sakayama (1987), Sasaki and Matsuo (1990), Hishida *et al.* (1992), Shibamoto *et al.* (1992), Ramirez *et al.* (1993), Spies and Ellis (1995). An example of an image from a 3-D resistivity tomogram is shown in (Figure 3).

Variations on the tomographic theme include anisotropic resistivity tomography (Sasaki, 1994), IP tomography (LaBrecque, 1991; Iseki and Shima, 1992), magnetic susceptibility tomography (Sakashita and Shima, 1993), and tomographic imaging of SP differences induced by fluid injection (Ushijima *et al.*, 1992). Resistivity tomographic schemes are also used to image core samples (Daily *et al.*, 1987; Dines and Lytle, 1981).

3.2. INDUCTIVE METHODS

Borehole induction methods with very large radii of investigation have been developed to search for deep ore deposits not intersected by drilling. To attain a large source moment, the transmitter is normally located at the surface, and the frequency is chosen low enough to prevent excessive skin depth attenuation in the host rock. This configuration is known as surface-to-borehole, and has successfully been used to depths as great as 3,000 m. Frequency-domain systems employing a surface loop include Noakes (1951), Ward and Harvey (1954), Salt (1966), Hohmann *et al.* (1978), and Worthington *et al.* (1981).

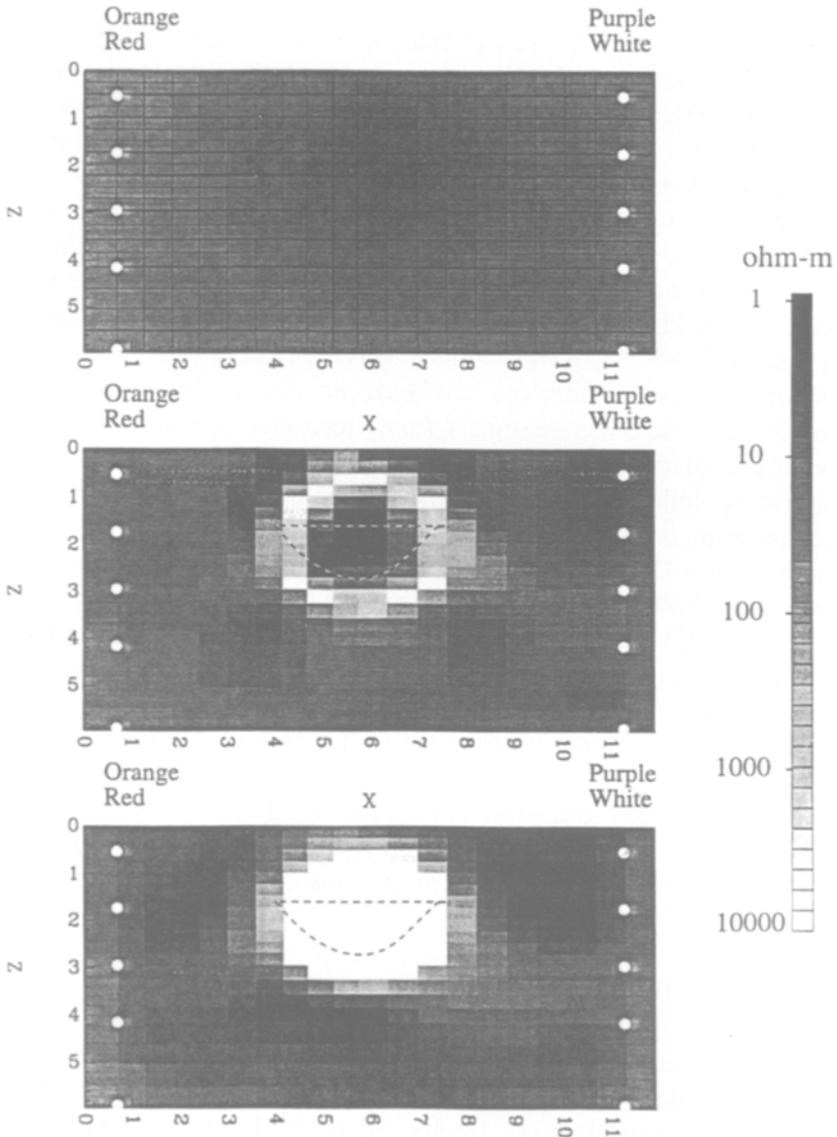


Figure 3. Cross-well resistivity images from three phases of an in-situ vitrification experiment. The three images were obtained from data collected before melting (top), during melting (middle), and after solidification (lower). White dots represent electrodes. 3-D resistivity data were collected in six boreholes surrounding the melt (Spies and Ellis, 1995).

Time-domain surface-to-borehole systems, first used in 1970 (Nabighian, 1984), have become more popular because of their broadband nature and relative ease of interpretation. Field examples of large-loop source, borehole receiver time domain EM surveys are given by Witherly (1980), Ogilvy (1983), Boyd and Wiles (1984), Dyck *et al.* (1985), Crone (1986), Boniwell (1986), Reed (1986), Levy and McNeill (1986), Eadie and Staltari (1987a), Asten *et al.* (1987), Bishop *et al.* (1987), Eadie (1987), Eadie and Staltari (1987b), Irvine (1987), Lane (1987), Mutton (1987), Richards (1987), Crone (1987), Robertson and Ascough (1991), Doe *et al.* (1991). The recent introduction of three-component receivers in the time-domain (Lee, 1986; Duncan and Cull, 1988; Hodges *et al.*, 1991; Cull, 1993) and frequency-domain (Worthington *et al.*, 1991; Pantze *et al.*, 1986; Cull and Cobcroft, 1986; Bourgeois and Bernard, 1991) has added much-needed directional capability.

Variations of the large surface source, borehole receiver geometry are possible. One interesting modification with a fixed borehole receiver and moving surface transmitter is described by Coggon and Clarke (1987). Applications of surface-to-borehole techniques in other fields include saline contaminant mapping (Asch and Morrison, 1989; Bevc and Morrison, 1991), and enhanced oil recovery (Spies and Greaves, 1991).

3.3. LOGGING TOOLS IN MINERAL EXPLORATION

Logging tools used in mining are similar to their petroleum counterparts described in Section 6, but are usually smaller in diameter and are not designed to be operated under high pressure. Borehole logging is routinely used for exploration for coal (Hoyer, 1991; Jiajin and Harvey, 1982; Kayal and Chistoffel, 1989; Peeters and Kempton, 1977; Reeves, 1976), and other minerals (Zablocki, 1966; Reeves, 1972; Reeves, 1976); Killeen and Mwenifumbo, 1987; Emilsson and Wanstedt, 1993; Hollyer *et al.*, 1991; Schoen, 1993). Descriptions of mineral logging in specific countries are Russia (Czubek, 1971), Czechoslovakia (Kobr, 1990) and France (Labert, 1981).

Induction logging tools developed specifically for mineral exploration are Clerc *et al.* (1983), Frignet (1986), Straub and Valla (1987). Attempts to increase the depth of investigation of induction logging tools by increasing the separation of source and receiver are described by Elliott (1961) and Smith and Hallof (1971). Simultaneously measurement of magnetic susceptibility and electrical conductivity can be made with an induction device (Scott *et al.*, 1981; Bristow, 1987).

Other mineral exploration logging tools are combined resistivity and IP (Tyne and Dagggar, 1990; Tyne *et al.*, 1985; Webster, 1986; Mwenifumbo, 1989).

Induction logging tools are finding an important application in environmental studies, e.g., contaminant mapping with induction logs (DeSimone and Barlow, 1993), and tracking salt in groundwater (Church and Friesz, 1993).

4. Radar

Borehole radar systems, which typically operate at frequencies of tens to hundreds of MHz, are used to probe rocks of very high resistivity, such as salt and granite. At these frequencies dielectric properties become important, the physics is best described by wave propagation, and relatively simple concepts such as ray paths and travel time can be used for interpretation. Borehole radar systems can operate in single-well mode (Bradley and Wright, 1987), detecting reflections from scatterers, or in cross-borehole mode (Lager and Lytle, 1977; Olhoeft, 1988), measuring attenuation or travel time. Standard tomographic inversion techniques (Dines and Lytle, 1979; Lytle and Dines, 1980) are readily applied to cross-well radar data.

Radar systems were first used in boreholes in the early 1970s to detect the boundaries of salt domes hundreds of meters distant (Holser *et al.*, 1972; Stewart and Unterberger, 1976; Halleux *et al.*, 1992; Nickel *et al.*, 1983; Unterberger, 1978), and have also been applied in coal seams (Cook, 1977; Coon *et al.*, 1981) and mining (Cook, 1977; Coon *et al.*, 1981; Nilsson, 1986). Borehole radar is routinely applied in such geotechnical applications as tunnel detection (Kong *et al.*, 1993; Lytle *et al.*, 1979; Moran and Greenfield, 1993) and characterization of fractures (Cook, 1977; Okada *et al.*, 1980; Coon *et al.*, 1981; Andersson *et al.*, 1989; Olsson and Nilsson, 1986; Olsson *et al.*, 1989; Olsson *et al.*, 1992; Chang, 1989; Sandberg, *et al.*, 1991; Holloway *et al.*, 1992).

5. Cross-borehole Electromagnetics

Tests of the underground detection of radio waves have been carried out intermittently since the 1920s, including measurements of the attenuation of radio-waves between boreholes in Germany in the 1930s (Rust, 1940). However, it was not until the Lytle and others in the late 1970s laid the theoretical foundation of geotomographic imaging that interest spread in the geophysical community. The earliest cross-well experiments in an oilfield environment used frequencies in the 1- 30 MHz range (e.g., Kretzschmar *et al.*, 1982; Witterholt and Kretzschmar, 1982; Witterholt and Kretzschmar, 1984), but covered relatively short distances.

Parallel to the developments in resistivity tomography, theoretical studies on electromagnetic propagation in resistive crustal layers (e.g., Wait, 1970; Wait and Spies, 1972) showed that the layers often form an efficient waveguide for propagation of EM waves over long distances. It was known that coal seams formed an effective waveguide that could be used for radio communication (e.g., Wait, 1976; Hill, 1984). The fact that radio waves could also be used to detect geological inhomogeneities in coal seams was soon recognized and the necessary technology developed (Shope, 1987; Shope *et al.*, 1986; Rogers *et al.*, 1987; Stolarczyk and Fry, 1989; Stolarczyk *et al.*, 1988; Stolarczyk, 1990). The technique, often termed the Radio Imaging Method (RIM), is being used in several countries (Thomson *et*

al., 1990; Vozoff *et al.*, 1993; Takacs, 1993; Young and Rogers, 1994) and employs hand-held loop antennae in mines or probes in boreholes. The RIM measurement is based on attenuation of the EM signal in the frequency range 50–500 kHz. Applications of RIM to other mining problems are described by Thomson, *et al.*, (1990), Thomson and Hind (1993), Thomson *et al.* (1992); McGaughey, 1991), and to tunnel detection by Mahrer and List (1995). There is, of course, an overlap in frequencies between RIM and cross-well radar referred to earlier. The term RIM is normally confined to continuous-wave measurements of signal attenuation, whereas radar measures discrete pulses in the time domain.

Radio-wave methods are also widely used in the (former) Soviet Union, and include borehole-to-surface and borehole-to-borehole attenuation (radio-wave shadowing) and reflection variants (e.g., Petrovsky, 1971; Chmelevskoy and Bor-darenko, 1989).

Until recently, interpretation of EM tomographic data has normally employed standard ray-tomographic inversion techniques, which may not be accurate at the frequencies employed. Nekut (1994) describes the conditions under which ray-theoretic approaches are valid. Improved interpretation techniques for the diffusion regime are described by Sena and Toksoz (1990); Rogers *et al.*, 1993; Alumbaugh, 1994; Alumbaugh and Morrison, 1994, 1995; Torres-Verdin and Habashy, 1994; and Newman, 1995).

To extend the application of cross-well electromagnetics to a conductive or lossy earth it is necessary to employ lower frequencies. Field systems designed for low frequencies (1 kHz to 50 kHz) are currently being developed (Wilt *et al.*, 1991, 1995; Osato and Takasugi, 1992; Gasnier *et al.*, 1994; Sakashita *et al.*, 1994; Sasaki *et al.*, 1994) for reservoir characterization and geotechnical applications. There is trade-off between resistivity, borehole separation and optimal frequency (Spies, 1992; Spies and Habashy, 1995); however, even in relatively conductive sedimentary rocks, measurements are possible between boreholes spaced many hundreds of meters apart. Several groups are also developing three-component receivers.

5.1. ELECTROMAGNETIC MEASUREMENTS THROUGH STEEL CASING

The presence of steel well casing in most oil fields has hindered the use of cross-well electromagnetics. Various numerical studies and field tests (Uchida *et al.*, 1991; Spies, 1992; Wu and Habashy, 1994; Wilt and Ranganayaki, 1990) suggest that it may be possible to measure magnetic fields through steel casing at sufficiently low frequency. Nekut (1995) describes the use of resistive sections between casing joints that can be used as electric dipoles for high-frequency cross-well measurements.

5.2. USE OF STEEL WELL CASING AS A SOURCE FOR SURFACE MEASUREMENTS

Steel casing used as a source electrode is a blend of *mise-à-la-masse* and d.c. tomography, and is often used to increase the depth of investigation of electrical

studies around an injection or production well. Examples in oil exploration are given by Rocroi and Koulikov (1985); Le Masne and Poirmeur (1988), Goldman (1990), Ushijima *et al.* (1992b), Sugimoto (1992).

6. Petroleum Well Logging

The prime catalyst for the rapid technological development of borehole electrical and electromagnetic logging has been the need to accurately assess hydrocarbon content in boreholes drilled for petroleum. Unlike the small-diameter mineral exploration boreholes that are usually cored, the larger-diameter boreholes employed in the petroleum industry have multiple uses: exploration for hydrocarbons, assessment of productivity of reservoirs, and production of the hydrocarbons.

Well logging technology now supports a major industry. Literature searches reveal at least 10,000 references in English related to borehole logging techniques and interpretation, many of which are in publications of the Society of Prof. Well Log Anal. and its European counterparts.

This section will give a very brief overview of the electrical and EM techniques used in petroleum well logging, in order of increasing operational frequency. Only key references are given; the reader is referred to the many excellent texts (e.g., Serra, 1984, 1986; Hearst and Nelson, 1985; Jorden and Campbell, 1986; Ellis, 1987; Labo, 1987), reprint volumes (SPWLA, 1992) and bibliographies (SPWLA, 1985; Maute, 1992; Prensky, 1992) for more detailed information.

6.1. THE DRILLING ENVIRONMENT

Electrical and EM well logging tools are adapted to the drilling environment encountered in petroleum provinces. Petroleum wells are routinely drilled to depths of 5,000 m or more; often multiples wells are drilled from the same platform and deviated to intersect different parts of the reservoir. Heavy drilling mud is used in the drilling process to prevent blowouts and excess fluid loss into the formation, and its density is such that overpressure is maintained during the entire drilling process. Drilling mud can be water-based or oil-based, and is charged with dense minerals like barite and conditioned with gels such as bentonite. Oil-based muds are used to prevent shales from spalling and blocking the well. The resistivity of the drilling mud varies widely, from less than 0.1 ohm-m for salty muds, to thousands of ohm-m for oil-based muds. The range of resistivities of sedimentary formations is also large, from less than 0.1 ohm-m in many brine-filled sands, increasing to 1 to 10 ohm-m in many shales, to tens of thousands of ohm-m in some carbonates.

In permeable formations the drilling fluid rapidly flows into, or invades, the formation. Clay platelets in the drilling mud build up on the borehole wall, eventually forming a relatively impermeable barrier (the mud cake) that inhibits further fluid loss. The mud cake can reach thicknesses of several centimeters opposite

high-permeability zones. The invaded fluid, known as the mud filtrate, forces the natural or connate formation fluids some distance back into the formation, leaving behind a certain amount of irreducible fluid. In some cases the invaded zone can be up to 1 or 2 m in diameter.

Historically, the primary purpose (but not the first use) of electrical and EM logging methods was to identify hydrocarbon-bearing sands. Sands and shales are discriminated with the SP (and gamma-ray) logs, and oil or gas zones identified by their higher resistivities. Resistivity and induction logs are used to determine the true resistivity of the formation and, together with independent estimates on the rock porosity obtained from other techniques, determine the percentage of oil or gas filling the pore space, or conversely, the water saturation.

Logging tools evolved to deal with dramatic variations in resistivity of drilling mud and formation, environmental realities such as borehole breakouts and changes in borehole diameter, variable invasion, and the need for detailed information on a wide range of lithologies. Logging technology and geological interpretation has advanced rapidly, and electrical and EM techniques now provide detailed resistivity images of the borehole wall, estimates of pore size distribution and fracture and hydrocarbon analysis.

6.2. ELECTRICAL PROPERTIES OF SEDIMENTARY ROCKS

The electrical properties of sedimentary rocks have been studied for many years (Archie, 1942; Wyllie, 1957; Waxman and Smits, 1968; Sen, 1991; Sen *et al.*, 1981). Electrical conduction at low frequencies is dominated by ionic conduction in the pore fluids, and depends strongly on water salinity and saturation, porosity, and the effective conduction path length, or tortuosity. In shales the relationship becomes more complex; conduction is largely due to exchangeable ions on the surface of clay particles (charge polarization). At higher frequencies dipolar, atomic and electronic polarization play important roles.

The electrical properties of a rock are normally described in terms of electrical conductivity σ and electric permittivity or dielectric constant ϵ . In the most general case, both quantities are complex and dispersive, and cannot be separated. The choice of terminology is not clear, and has led to many discrepancies in the literature (Fuller and Ward, 1970).

Depending on the frequency regime, most workers choose specific terms for the in-phase and quadrature components that relate the measured electric field intensity and current density. Below 100 MHz, where $\sigma/(\omega\epsilon)$ is normally less than 1, the in-phase component is normally described as a conductivity term, and the quadrature as an electric permittivity term. Above 100 MHz it is customary to express the electrical properties as complex permittivity, where the imaginary part of the measured quantity is the conductivity (divided by frequency).

The conductivity of most rocks increases slowly with frequency until around 100 MHz, due to dipolar relaxation of water at a length scale much smaller than

the pore size. Around 1 GHz, conductivity becomes proportional to water fraction. Above 1 GHz, conductivity increases further due to the contribution of relaxation of water molecules, which peaks at about 16 GHz.

The effective permittivity at low frequencies is dominated by surface effects due to interstitial clays (often termed induced polarization below 1 kHz). Electric permittivity is related to the pore concentration of clays in sand pores, and allows estimation of the cation exchange capacity of the rock (Vinegar and Waxman, 1984). It reaches stable values between 0.2 GHz and 2 GHz, and is much higher for rocks saturated with water than with hydrocarbons. Logging measurements of permittivity made at frequencies between 20 MHz and 1 GHz are used to evaluate hydrocarbons in the presence of fresh, resistive formation water.

At still higher frequencies the interaction of the rock's material with electromagnetic radiation leads to absorption peaks or resonances at frequencies characteristic of various molecular oscillations, including vibrational and electronic modes. Molecular oscillations of water and hydrocarbons are utilized in optical logging methods, described later.

6.3. SPONTANEOUS POTENTIAL LOG

Spontaneous potentials arise from a variety of sources, including gradients in ionic concentration (electrochemical potential) and filtration (electrokinetic potential). The SP measurement (Doll, 1948; Wyllie, 1948) is very simple – basically a recording of the potential difference between an electrode in the borehole and an electrode at the surface – but is one of the most widely used for petroleum well logging.

The electrochemical potential originates at the junction of two solutions with different salinity (the mud filtrate and the formation fluid), at the outer boundary of the invaded zone. The concentration difference sets up an ionic current path through the formation into adjacent beds with different electrochemical properties (such as shale), forming a closed current path through the fluid-filled borehole. In sands and shaley sands SP values vary from -120 mV to $+40$ mV, compared to values measured next to adjacent shale beds. Filtration potential (Gondouin and Scala, 1958) is normally smaller than the electrochemical potential, and is highly dependent on the water conductivity.

The SP log records the difference between the shale and more permeable formations, and generally gives a good approximation of the electrochemical potential. It provides an independent estimate of the water resistivity or clay cation exchange capacity in the formation, as well as a permeability indicator.

6.4. LOW-FREQUENCY ELECTRODE TOOLS

The evolution of electrode tools, from the normal array used in the 1920s to the focussed laterologs developed in the ensuing fifty years is shown in (Figure 4).

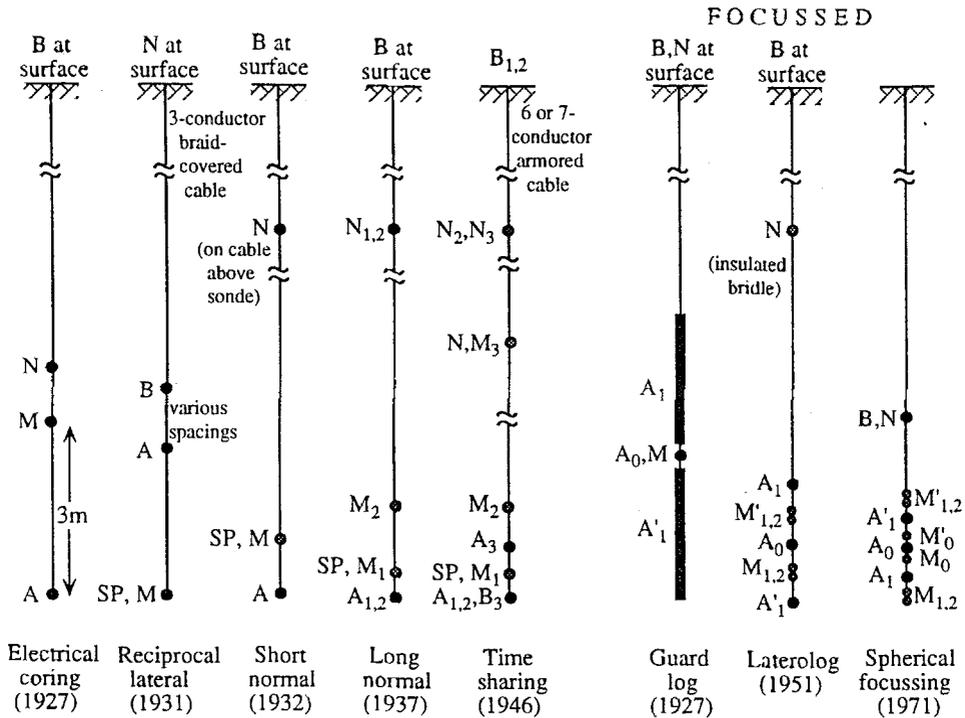


Figure 4. Evolution of logging electrode arrays. Unfocussed arrays are shown on the left; focussed on the right. A and B are current electrodes, M and N are potential electrodes (after Segesman, 1980).

6.4.1. Unfocussed Devices

The earliest electrode configuration, the normal array, consisted of a single current and potential electrode in the well, with returns at the surface (Figure 4). Low frequency a.c. currents (a few tens of hertz) are used to prevent electrode polarization. The equipotential pattern is strongly influenced by the borehole and invaded zone, and has a relatively shallow depth of investigation. The lateral array effectively measures the potential gradient downhole, and has a greater depth of investigation than the normal array. For many years the term electrical coring (Schlumberger *et al.*, 1932) was used to describe the combination of normal and lateral devices. The Microlog (Doll, 1950) is a pad tool with a very shallow depth of investigation (less than 5 cm), used to identify mud cake buildup that characterize permeable zones

6.4.2. Focussed Resistivity

Devices that incorporate passive or active focussing were developed to minimize the undesirable influence of the borehole and provide a deeper, more reliable measurement. The concept of passive focusing using long guard electrodes dates back Schlumberger's work in 1927. The guard electrodes force current into the formation perpendicular to the hole by keeping all electrodes at a constant potential

(Owen and Greer, 1951). Early passively focused tools include the Guard and Proximity (Hamilton, 1960) logs.

Other passively focussed tools were devised to provide more detailed information on sedimentary features. The high resolution dipmeter (Allaud and Ringot, 1969) is a four-pad device that records four resistivity measurements around the borehole wall. Formation dip is determined by cross-correlation of the four resistivity tracks. The concept of high-resolution pad measurements evolved into electrical resistivity imaging tools, described in later in Section 6.7.

Active focusing techniques employ an array of electrodes that continually balance the potential along the tool so that current is directed into the formation perpendicular to the measuring current electrode. Also, small focussing electrodes can be used, and they can be combined with SP and induction tools. The success of the focusing concept can be seen by tracing the current line paths (Figure 5).

The Laterolog-7 (Doll, 1951) was the first short-electrode laterolog, and employed 7 electrodes. This was followed by the Laterolog-8 (Doll *et al.*, 1960) and spherically focussed tool. The dual laterolog (Suau *et al.*, 1972) combines deep and shallow measurements in a single tool, and is most suitable for high-contrast resistivity logging and salty muds. Other actively-focused tools, too numerous to mention here, have been introduced for specific markets. The basic requirements for these designs are a multiple depth of investigation that enables accurate computation of the invaded zone resistivity and deeper true formation resistivity, a reduced sensitivity to borehole effects, and good thin-bed resolution.

6.4.3. *Deep Measurements*

Several tools have been built to measure large distances from the well. A scaled-up normal array with electrode spacings up to 300 m and frequency lowered to 0.1 Hz known as ULSEL (ultra-long spaced electrical log) is described by Runge *et al.*, (1969). Its main use is to determine the distance to the flanks of salt domes.

6.5. ELECTROMAGNETIC LOGGING

Despite the success of the low-frequency electrode tools, induction tools have become the prevailing resistivity tool because of their greater depth of investigation and efficacy in high-resistivity oil-based muds. Doll invented the first induction tool in the 1940s (Doll, 1949); it was a three-coil device operating in the low-induction number regime (typically around 10 kHz), where the depth of investigation is proportional to source-receiver separation. The device operates with one source coil and two receiver coils wound in opposition so that the net free-space signal is zero. Later, additional transmitter or receiver coils were added to focus the zone of greatest sensitivity deeper in the formation (e.g., the deep induction). Two depths of investigation are provided by the dual induction design (Tixier *et al.*, 1963).

The advantage of operating in the low-induction number regime is that the received signal in-phase signal with the transmitter current (the so-called R-signal)

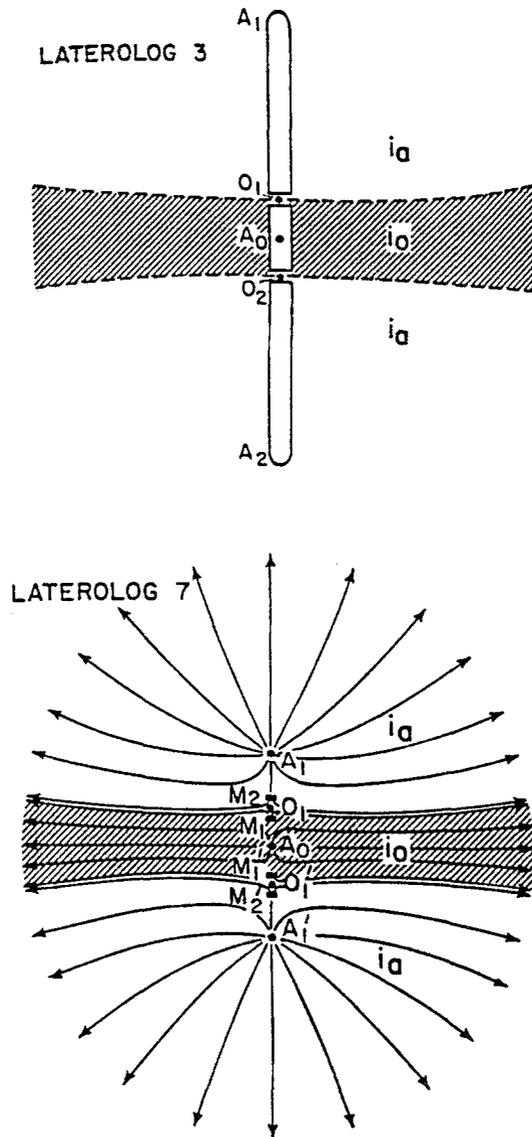


Figure 5. Two designs for current focussing with resistivity logging tools, used to reduce sensitivity to borehole effects and increase vertical resolution. An early three-electrode design from the 1920s (top) used two long guard electrodes (A_1 , A_2) kept at the same potential as the measuring electrode A_0 to passively focus the measuring current into the formation. Later designs utilized active focussing: the 7-electrode laterolog design (bottom) maintains a zero potential difference between the two pairs of potential electrodes M_1 – M_2 by continually adjusting the currents leaving A_1 and A_1' . Since the potential drop along the sonde in the vertical direction is zero, current from the measure electrode A_0 is focussed deep into the formation (from Suau *et al.*, 1972).

is directly proportional to formation conductivity. With the advent of better electronics and processing software it became possible to measure the small out-of-phase signal (quadrature or X-signal) caused by eddy currents in the formation and incorporate skin effect in interpretation (e.g., Barber, 1985). Recent developments include array induction tools operating with multiple coil spacings and frequencies with 5 or 6 depths of investigation (e.g., Martin *et al.*, 1984; Barber and Rosthal, 1991). With these tools it is possible to construct axisymmetric resistivity images of the first 1 or 2 m surrounding the borehole, considerably assisting with geological interpretation and simplifying identification of invasion.

6.6. ELECTROMAGNETIC PROPAGATION TOOLS

Electromagnetic propagation tools are used to distinguish between oil and resistive fresh formation water based on the large contrasts in their dielectric constants. The earliest tools (Calvert *et al.*, 1977; Poley *et al.*, 1978) were pad devices operating at 1.1 GHz, with a penetration depth of 2 to 10 cm. Later, mandrel tools operating at lower frequencies (around 25 MHz) with an array of receivers increased the depth of investigation up to 1 meter. However, interpretation is often complicated by strong dispersion in the MHz frequency range.

6.7. ELECTRICAL IMAGING

Borehole imaging is one of the most rapidly advancing fields in wireline logging. Wireline imaging devices produce images of the borehole wall that can be used to infer detailed geological information such as the geometric arrangement of rock layers, or structure, and sedimentological data on rock texture, fabric and facies type.

6.7.1. *High-resolution Shallow Devices*

Electrical imaging of the borehole wall emerged in the 1980s as an extension of dipmeter technology. Electrical imaging tools have multiple arms with an array of small button electrodes that contact the borehole wall and inject current into the formation (Ekstrom *et al.*, 1986; Straub *et al.*, 1991). Their maximum vertical and horizontal resolution is of the order of 5 mm. The current leaving each button is assumed to be directly proportional to the local conductivity. The conductivity data are displayed as a color image, which is unwrapped onto a projection of the borehole wall (Figure 6). A planar dipping feature shows up as a sinusoid from which the dip and strike can be uniquely determined.

The image contains bedding information crucial in sedimentological analysis (McGann *et al.*, 1988; Plumb and Luthi, 1986), facies characterization, and reservoir zonation (Luthi and Banavar, 1988). Also, porosity and mineralogical variations affecting the resistivity image are clearly seen in the image texture. An important application, especially in crystalline rocks, is mapping and characterizing fractures. Very thin fractures, filled with conductive drilling mud, become

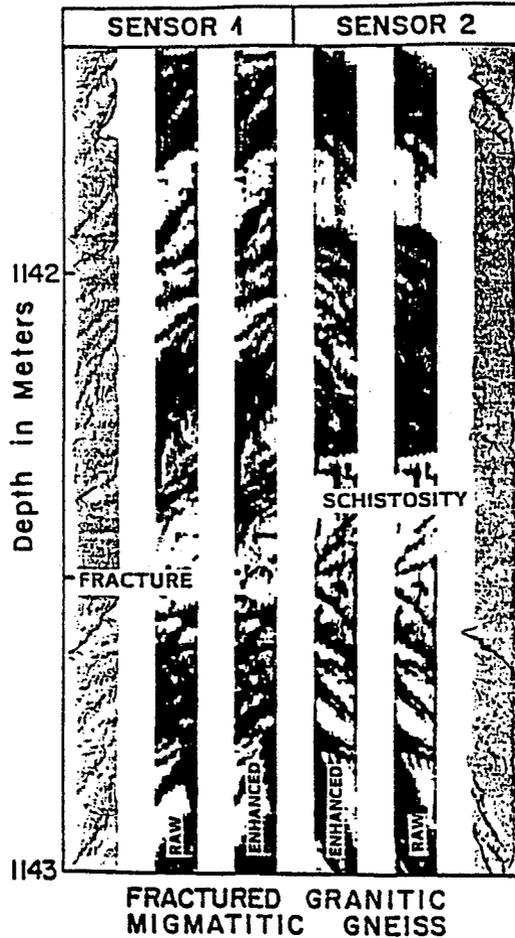


Figure 6. High-resolution resistivity image of the borehole wall recorded in the Cajon Pass scientific drillhole, California, showing fracture and foliation patterns in crystalline granitic gneiss (from Pezard and Luthi, 1988).

prominent features on microelectrical images (Dennis *et al.*, 1987; Laubach *et al.*, 1988; Luthi and Souhaité, 1990). The same is true of carbonates and other rocks with dissolution macro-porosity (Badr and Ayoub, 1989). Other applications are identification of faults (Koepsell *et al.*, 1989) and characterization of crystalline rocks (Pezard, 1992; Pezard and Luthi, 1988; Draxler *et al.*, 1990). Key papers on borehole imaging are reprinted in Paillet *et al.* (1990).

6.7.2. Deeper-reading Calibrated Imaging Devices

High-resolution imaging devices have a shallow depth of investigation and are uncalibrated. These issues are addressed in a new calibrated azimuthal resistivity tool based on a dual laterolog design, which incorporates 12 or more electrodes arranged circumferentially around the tool (Davies *et al.*, 1992). Images from these

tools are not as sharp as those provided by the high-resolution devices, but are useful for quantitative estimates of small-scale resistivity structure not resolvable on conventional electrical logs (Rauen and Lastovickova, 1994).

6.8. NUCLEAR MAGNETIC RESONANCE (NMR)

Nuclear magnetic resonance, originally termed nuclear induction (Bloch, 1946; Bloch *et al.*, 1946), is based on the precession of atomic nuclei in a d.c. magnetic field. NMR logging tools first became available in the 1960s (Brown, 1960; Hull and Coolidge, 1960). The basic NMR tool measures the relaxation time of hydrogen nuclei in the pore space of a rock and hence gives a direct measure of the free fluid in the rock (the hydrogen in water and hydrocarbons), as well as viscosity and permeability. The decaying magnetic field amplitude can be interpreted as a superposition of a suite of exponentials, each corresponding to a typical pore size. By a suitable choice of observation window it is possible to determine the pore size distribution and discriminate between fluids bound to surfaces (such as the water in shales) which have much faster relaxations, and fluids in pore space.

Early NMR logging tools measured atomic precession in the earth's magnetic field, and required doping of the drilling mud to reduce its signal. New pulsed NMR tools (Cooper *et al.*, 1980; Jackson, 1984) use strong permanent magnets. NMR logs can provide robust estimates of porosity that is independent of lithology (Miller *et al.*, 1990; Morriss *et al.*, 1993). Jackson and Matthews (1993) gives a bibliography of 500 references related to NMR logging.

6.9. OPTICAL METHODS

A new development in borehole measurements is optical spectroscopy, based on the absorption of light as a function of wavelength. Measurements of the absorption spectra in the near-infra red and visible range (\sim micron or 10^{14} Hz) are used to differentiate between fluids sampled in a borehole (Mullins *et al.*, 1992; Smits *et al.*, 1993).

6.10. CORROSION IN CASING

Corrosion of steel casing is a major expense and hazard in hydrocarbon, geothermal and water wells. Wireline logging tools that detect corrosion include mechanical (caliper), acoustic, electromagnetic and electrochemical (Cryer *et al.*, 1987; Monrose and Boyer, 1992). One electromagnetic corrosion tool employs flux leakage detection using a low-frequency magnetic field and a second measurement at 1 kHz to delineate inner surface defects (Cuthbert and Johnson, 1974). A second group of tools measures the in-phase and quadrature response at a frequency low enough (typically 10 Hz) that the response varies with the casing thickness (Smith, 1981). Other tools measure polarization potentials on the inner casing surface due to corrosion electrochemical cells.

7. Emerging Technologies

7.1. LOGGING WHILE DRILLING (LWD)

In standard logging the sonde is lowered on a wireline cable down the borehole after drilling. It was recognized in the early 1930s that information on the drilling process could be conveyed to the driller via the drilling mud using mud pulse telemetry. The first downhole drilling measurements were directional (azimuth, inclination, and tool face), progressing to resistivity (basically a 16-inch short normal) in the late 1970s (Buchholz, 1982). In the mid-1980s 2-MHz electromagnetic propagation tools were introduced (Rodney *et al.*, 1983; Coope *et al.*, 1984), which were well-suited to conductive formations and oil-based drilling muds.

In the last few years LWD resistivity technology has evolved rapidly (Allen *et al.*, 1989) to include both multi-spacing and multi-frequency propagation tools and resistivity tools similar to laterologs which can operate in oil-based muds. These tools use toroids to induce currents on the drill collar which then leak out into the formation. The sensing elements in all LWD tools up until recently were spaced 15 to 30 m behind the drill bit, which meant that geological information from the bit location was not received in real time. Most recently the resistivity measurement has been moved within 1 m of the bit, with the bit itself becoming part of the electrical circuit. The ability of measuring resistivity "at the bit" has motivated a major change from "geometric steering" to "geological steering" (Figure 7) (Bonner *et al.*, 1993). This technology now makes it possible to steer a horizontal well within a meter of a geological horizon, over distances of many kilometers, and dramatically improve the efficiency of draining oil reservoirs.

7.2. RESISTIVITY THROUGH CASING

Measuring the resistivity of rocks behind steel casing is a formidable challenge, because the conductivity of steel casing (6×10^6 S/m) is 6 to 8 orders of magnitude higher than that of typical formations. The concept of injecting current into casing and measuring the very small potential changes due to current leakage into the formation can be traced to the 1930s (Alpin, 1939). However, the measurements have only recently become feasible due to advances in electronics and techniques for compensating for variations in casing resistivity and thickness. Numerical and practical studies are described by Kaufman (1990); Kaufman and Wightman (1993), Klein and Martin (1993) and Schenkel and Morrison (1994). Experimental tools that measure resistivity through steel casing with stationary measurements are currently in the testing phase (e.g., Vail *et al.*, 1993), and initial results are encouraging.

The possibility of making inductive measurements through casing has also received attention (Augustin *et al.*, 1989; Uchida *et al.*, 1991).

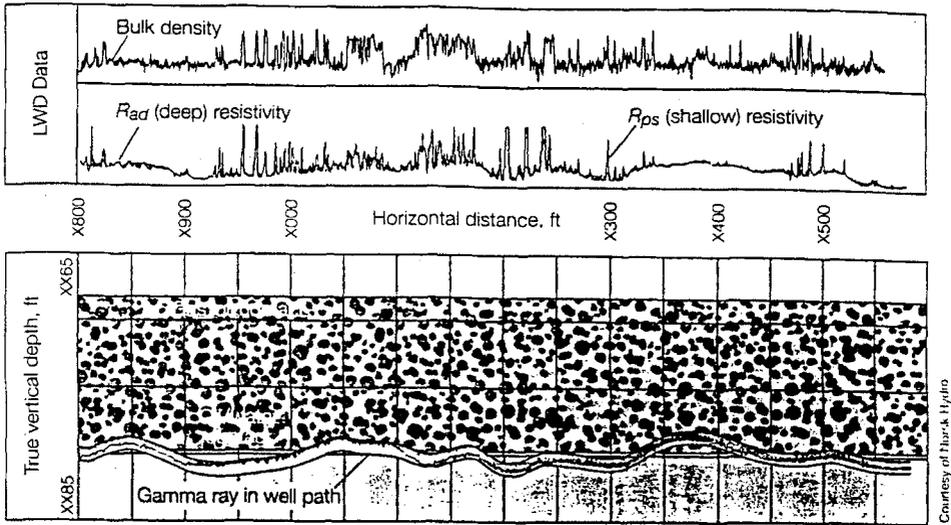


Figure 7. Geological steering along the top of an oil-water contact in the North Sea using resistivity and density logging-while-drilling measurements (from Bonner *et al.*, 1993)

8. Measurements in Deep Crustal Boreholes

Many of the deep boreholes drilled for purposes of scientific research are fully or partially cored, but data on rock properties in-situ (at borehole temperature and pressure) can only be obtained from logs. Borehole electrical and EM techniques used in deep crustal boreholes are similar to those used in commercial applications, except tools must usually be modified to withstand the very high temperatures and pressures encountered in deep wells, and the size must be reduced for the slim holes (<12.7 cm) often used in scientific drilling programs. Standard logging tools developed for the petroleum industry are rated to 175 °C and 140 MPa. Certain tools developed for hostile environmental logging (HEL) conditions are designed to operate at 260 °C and 170 MPa. Government and research institutions working with vendors have modified many of the standard tools, and designed new tools, to meet the needs of deep scientific drilling.

The following section summarizes electrical and EM logging measurements used in several of the deep scientific drilling boreholes. Many are standard logging tools, but some measurement such as magnetic variations are unique to research boreholes.

8.1. KTB, GERMANY

An extensive literature exists for the two KTB (Kontinentales Tiefbohrprogramm der Bundesrepublik) boreholes in Germany, in the form of formal reports and many papers in the journal *Scientific Drilling*. The first borehole is known as the KTB-VB, was drilled as a pilot to a depth of 4 km. The main borehole, the KTB-

Oberpfalz HB was spudded in 1990. It has passed 8 km and is planned for 10 km (the original plan was for 12-14 km but the temperatures were found to be much hotter than expected). A good review of progress in recent scientific drilling is given by Andrews and Pyle (1991).

Major suites of logging tools that have been run in the KTB boreholes include galvanic and inductive EM, as well as density, spectral gamma, thermal conductivity, remanent magnetization and magnetic susceptibility, porosity, stress relaxation, acoustic emissions, sonic and nuclear geochemical logging (Bram and Hänel, 1991). Borehole EM and electrical methods applied include 3-D magnetics, gradient magnetics, IP, SP, and electrical imaging (Draxler *et al.*, 1990).

Surface geophysical investigations in the vicinity of the KTB, which include over 100 MT and CSAMT soundings, identified a large SP anomaly (900 mV) and anomalous low conductivity with lateral variations below 4 km depth (Haak *et al.*, 1991). Resistivities determined from logging range from 1000 to 100,000 ohm-m to about 4 km depth, when they abruptly drop to values as low as 1 ohm-m where the borehole intersects sub-vertical pyrite- and graphite-bearing cataclastic zones. Bremer *et al.*, (1992) discusses differences in electrical conduction mechanism in sedimentary rocks and crystalline rocks found in the KTB. Crystalline rocks are dominated by surface effects caused by the very small (< 100 nm) pore size rather than volume effects that influence rocks with larger pore sizes.

The average resistivity of the upper 4 km from surface EM is between 100 and 500 ohm-m, much lower than the borehole logs which are above 1000 ohm-m for 80 percent of the depth interval. Kück (1992) reconciles the discrepancies between surface EM and borehole measurements by analyzing resistivity data from laterologs, induction logs and microfocussed logs, which cover a wide range of spatial scales. By using a model of parallel conductance to integrate data at different scales, the average resistivity is interpreted to be 300 ohm-m.

The high conductivity at 7 km depth is determined from core samples (Rauen *et al.*, 1994) to be caused by increased graphite and sulphide mineralization, and saline inflows from pores and cracks. However, Rauen *et al.* (1995) also found that in situ resistivity from 6 km to 3 km depth, measured with a deep-reading resistivity imaging log, is higher than that measured on core samples, and attributed the disparity to pressure release during core recovery and the filling of microcracks with water. Rauen *et al.* (1995) also used the deep resistivity image to study electrical anisotropy, which ranged between $\lambda = 1$ and 1.5 (core measurements were 1.2 to 1.3 for amphibolites and lamprophytes to 2.8 for foliated gneiss). High-resolution resistivity images were used to study fractures, dip and the post-orientation of cores (Draxler *et al.*, 1990).

An improved SP tool rated at 300 °C and 150 MPa was developed (Winter *et al.*, 1991) to map extension of the surface SP anomaly to depth. The SP anomalies were attributed to oxygen fugacity and graphite in combination with redox potential. SP was also used to monitor electrokinetic effects stimulated by hydraulic pumping (Stoll, 1994).

IP logging measurements in the KTB pilot borehole (Grinat, 1991; Vogelsang *et al.*, 1992) identified strong metallic polarization from sulphide and graphite, which is evenly distributed throughout the crystalline rock, with higher concentrations in fracture zones.

A mise-à-la-masse experiment using the steel casings of the pilot and main boreholes as current electrodes and mapping the potential at the surface is described by (Stoll, 1993). He traced a conductive zone 100 m wide intersecting the main borehole between 250 m and 1500 m depth.

Measurements of the time-varying vertical electric field (E_z) were made by (Bahr and Eisel, 1990) who observed 4 mV of excursion between the surface and 4000 m depth, indicating lateral changes in conductivity. One of the few successful tests of the vertical magnetic gradient method (VGM) was conducted in the KTB (Spitzer, 1993; Steveling *et al.*, 1991). Magnetic-field measurements were made at the earth's surface and at 3000 m depth using a triaxial fluxgate magnetometer rated to 70 MPa and 100 C, at periods between 10 and 6000 s. Analysis of the VGM data showed that the surface telluric fields at the KTB site are strongly distorted by local conductivity anomalies, biasing conventional MT data interpretation.

8.2. GRAVBERG, SWEDEN

A detailed study of the electrical resistivity of the Gravberg-1 deep well in the Siljan impact structure in Sweden is described by Pedersen, *et al.*, (1992), where laterologs were run to a depth of 6100 m. MT interpretations were that the upper crust to be 10,000 ohm-m to a depth of around 6 km, where the resistivity of an impact-related unit decreased to about 1000 ohm-m. Below 6 km the resistivity was interpreted to be about 300 m. The borehole measurements confirmed the MT interpretations and showed that zones of increased conductivity are related to fracture zones with increased porosity, and that below 5.4 km the pore fluids are highly saline.

8.3. CAJÓN PASS

High-resolution resistivity imaging logs were run in the Cajón Pass scientific well in California, between 850 m and 1820 m depth (Pezard *al.*, 1988). The images were used for textural analysis of the igneous rocks, and identification and mapping of open or mineralized fractures.

8.4. TOA BAJA, PUERTO RICO

An intriguing use of resistivity logs in the Toa Baja Scientific Drill Hole, Puerto Rico, is described by Maltezos and Anderson (1991), who identified Milankovich cycles in sedimentary history from an analysis of the power spectra of resistivity logs of interbedded limestone, sandstone and shale in the upper 600 m of the borehole.

9. Summary

By locating sources or sensors in boreholes, the earth scientist can vastly improve the utility and range of investigation of geophysical techniques compared to what can be achieved when measurements are restricted to the earth's surface. On the smallest scale, detailed resistivity images of the borehole wall reveal sedimentological textures and fabrics that often substitute for core. Larger scale measurements provide bulk rock properties up to and above reservoir scale. Source and receivers may be located in separate boreholes to image the resistivity distribution between the boreholes, and map the migration of fluids over time.

Borehole electrical and electromagnetic logging technology has reached the level of technological sophistication that we can determine detailed electrical properties as well as lithology, dip, fracture pore size distribution and fluid content. Indeed, it can be argued that accurate petrophysical assessments can only be made in boreholes, where rocks are under natural conditions. The fastest growing area in borehole techniques is that of measurement while drilling, which enables many of the conventional logging techniques to be applied in real time during the drilling process, and the borehole to be steered along narrow stratigraphic intervals.

Acknowledgements

Many people assisted with material for this review paper, and I am indebted to authors who provided me with preprints of their work. Others, such as Phil Nelson, Misac Nabighian, Reza Taherian, Jay Tittman, Michael Oristaglio, and Jim Wait, provided many helpful suggestions and guidance.

References

- Allaud, L. A. and Martin, M. H.: 1977, *Schlumberger, the History of a Technique*, John Wiley and Sons, New York.
- Allaud, L. A. and Ringot, J.: 1969, 'The High Resolution Dipmeter Tool', *The Log Analyst* **10**, 3–11.
- Allen, D., Bergt, D., Best, D., Clark, B., Falconer, I., Hache, J.-M., Kienitz, C., Lesage, M., Rasmus, J., Roulet, C. and Wraight, P.: 1989, 'Logging While Drilling', *Oilfield Review* **1**, 4–17.
- Alpin, L. M.: 1939, 'The Method of Electric Logging in the Borehole With Casing', U.S. patent N56026.
- Alumbaugh, D. L. and Morrison, H. F.: 1994, 'Electromagnetic Conductivity Imaging With an Iterative Born Inversion', *IEEE Trans. Geosci. Rem. Sens.* **31**, 758–763.
- Alumbaugh, D. L. and Morrison, H. F.: 1995, 'Crosswell Electromagnetic Tomography: Theoretical and Practical Considerations for Cylindrical geometry', *Geophysics* **60**, 846–870.
- Andersson, K. P., Andersson, P. M., Gustafsson, E. and Olsson, O.: 1989, 'Mapping Groundwater Flow Paths in Crystalline Bedrock Using Differential Radar Crosshole Tomography Measurements Utilizing Saline Tracers', *Minerals and Geotech. Logging Soc., 3rd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper H, 117–125.
- Andrews, R. S. and Pyle, T.: 1991, 'A Survey of Recent Technology Development in International Continental Scientific Drilling Program', *Scientific Drilling* **1**, 310–323.

- Archie, G. E.: 1942, 'The Electrical Resistivity Log as an Aid in Determining Some Reservoir Characteristics', *Trans. AIME*, 54–62.
- Asch, T. and Morrison, H. F.: 1989, 'Mapping and Monitoring Electrical Resistivity With Surface and Subsurface Arrays', *Geophysics* **54**, 235–244.
- Asten, M. W., 1991, 'Field Examples of the Downhole MMR Method and Comparison With the TEM Method: Appendix to 'The Magnetometric Resistivity Method', by R. N. Edwards and M. N. Nabighian, in M. N. Nabighian (ed.), *Electromagnetic Methods in Applied Geophysics*, Soc. Expl. Geophys., Tulsa, 99–104.
- Asten, M. W., King, A. and Peacock, J.: 1987, 'Sign Changes in DHEM Surveys for Cindered Coal in the Sydney Basin', *Expl. Geophys.* **18**, 319–323.
- Augustin, A. M., Kennedy, W. D., Morrison, H. F. and Lee, K. H.: 1989, 'A Theoretical Study of Surface-to-borehole Logging in Cased Holes', *Geophysics* **54**, 90–99.
- Bacon, L. O.: 1965, 'Induced-polarization Logging in the Search for Native Copper', *Geophysics* **30**, 246–256.
- Badr, A. R. and Ayoub, M. R.: 1989, 'Study of a Complex Carbonate Reservoir Using the Formation Microscanner (FMS) Tool', *Soc. Petr. Eng., Proc. Middle East Oil Conf.*, Paper 19877, 507–516.
- Bahr, K. and Eisel, M., 1990, 'Vertikale Tellurische Pulsationen in der KTB Vorbohrung: Laterale Leitfähigkeitskontraste und Vertuelle Zeitliche Variationen des Eigenpotentials', in K. Bram, J. K. Draxler, W. Kessels and G. Zoth (ed.), *KTB Report 90-6a; Grundlagenforschung und Bohrlochgeophysik (Bericht 10)*, Projektgruppe Kontinentales Tiefbohrprogramm der Bundesrepublik Deutschland am Niedersächsischen Landesamt für Bodenforschung, Stuttgart, Germany, 179–189.
- Barber, T. D.: 1985, 'Introduction to the Phasor Dual Induction Tool', *60th Soc. Petrol. Eng., Ann. Conf.*, SPE 12049.
- Barber, T. D. and Rosthal, R. A.: 1991, 'Using a Multiarray Induction Tool to Achieve High-resolution Logs With Minimum Environmental effects', *66th Soc. Petrol. Eng. Ann. Conf.*, SPE 22725.
- Barus, C., 1882, 'On the Electrical Activity of Ore Bodies', in G. F. Becker (ed.), *Geology of the Comstock Lode and the Washoe District*, U. S. Geol. Surv. Monog., 309–367, 400–404.
- Bevc, D. and Morrison, H. F.: 1991, 'Borehole-to-surface Electrical Resistivity Monitoring of a Salt Water Injection Experiment', *Geophysics* **56**, 769–777.
- Bishop, J. R., Lewis, R. J. G. and Macnae, J. C.: 1987, 'Down-hole Electromagnetic Surveys at Renison Bell, Tasmania', *Expl. Geophys.* **18**, 265–277.
- Bloch, F.: 1946, 'Nuclear Induction', *The Phys. Rev.* **70**, 460.
- Bloch, F., Hansen, W. W. and Packard, M.: 1946, 'Nuclear Induction', *The Phys. Rev.* **69**, 127.
- Boniwell, J. B., 1986, 'Downhole Pulse EM – Two Recent Field Experiences', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Canada, Paper 85–27, 297–306.
- Bonner, S., Burgess, T., Clark, B., Decker, D., Orban, J., Prevedel, B., Luling, M. and White, J.: 1993, 'Measurements at the Bit: A New Generation of MWD Tools', *Oilfield Review* **5**, 44–54.
- Bourgeois, B. and Bernard, J.: 1991, 'Application of a Surface-to-borehole Frequency EM Method for the Detection of Deep Conductive Orebodies: A Test Study in the Iberian Pyrite Belt', *53rd Mtg. Eur. Assoc. Expl. Geophys., Abstracts*, pp. 372–373.
- Bradley, J. A. and Wright, D. L.: 1987, 'Microprocessor-based Data Acquisition System for a Borehole Radar', *IEEE Trans. Geosci. Rem. Sens.* **GE-25**, 441–447.
- Bram, K. and Hänel, R.: 1991, 'The German Continental Deep Drilling Program (KTB): An Introduction to Related Logging Activities', *Scientific Drilling* **2**, 55–57.
- Brant, A. A., 1966, 'Examples of Induced-polarization Field Results in the Time Domain', in S. M. Comm. (ed.), *Mining geophysics*, Soc. Expl. Geophys., Tulsa, 288–305.
- Bremer, M., Kulenkampff, J. and Schopper, J. R.: 1992, 'An Attempt of Deterministic Interpretation of KTB-Oberpfalz-VB Standard Logs', *Scientific Drilling* **3**, 6–15.
- Bristow, Q.: 1987, 'A Multi-frequency Slim Hole Inductive Conductivity and Magnetic Susceptibility Probe', *Minerals and Geotech. Logging Soc., 2nd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper S, pp. 217–225.

- Brown, B. H., Barber, D. C. and Seagar, A. D.: 1985, 'Applied Potential Tomography: Possible Clinical Applications', *Clin. Phys. Physiol. Meas.* **6**, 109–121.
- Brown, R. J. S.: 1960, 'Nuclear Magnetism Logging', *J. Petr. Tech.* **219**, 199–207.
- Buchholz, C. W.: 1982, 'Continuous-wave Mud Telemetry', *Technologies for Measurement While Drilling, Proc.*, Marine Board Comm. Engin. Tech. Systems, National Research Council, pp. 87–105.
- Calvert, J. T., Rau, R. N. and Wells, L. E.: 1977, 'Electromagnetic Propagation - A New Dimension in Logging', *6th Formation Evaluation Symp. Trans.*, Canadian Well Logging Soc. paper M, pp. 1–16.
- Chang, H.: 1989, 'Field Test Results of a Borehole Directional Radar', *Minerals and Geotech. Logging Soc., 3rd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper I, pp. 127–132.
- Chmelevskoy, V. K. and Bordarenko, V. M.: 1989, *Elektrorazvedka, Spravochnik Geofizika (Electrical Prospecting, Geophysical Reference)*, Nedra, Moscow.
- Church, P. E. and Friesz, P. J.: 1993, 'Deleation of a Road-salt Plume in Ground Water, and Travel-time Measurements for Estimating Hydraulic Conductivity by use of Borehole-induction Logs', *Minerals and Geotech. Logging Soc., 5th Intern. Symp. on Geophysics for Minerals, Geotech. and Environmental Applications, Proc.*, Soc. Prof. Well Log Anal., paper Y, pp. 1–16.
- Clerc, G., Frignet, B. and Tabbagh, A.: 1983, 'Transmitter-receiver Induction Probes and Techniques Developed for Surface and Borehole Measurements', *J. Geomag. Geoelectr.* **35**, 443–454.
- Coggon, J. H. and Clarke, E. H.: 1987, 'The Fixed Receiver Electromagnetic (FREM) Method for Drill Hole Surveys', *Expl. Geophys.* **18**, 305–311.
- Conklin, H. R.: 1917, 'Prospecting with Electricity', *Eng. Mining J.* **104**, 339–340.
- Cook, J. C.: 1977, 'Borehole-radar Exploration in a Coal Seam', *Geophysics* **42**, 1254–1257.
- Coon, J. B., Fowler, J. C. and Schafers, C. J.: 1981, 'Experimental Uses of Short Pulse Radar in Coal Seams', *Geophysics* **46**, 1163–1168.
- Coope, D., Shen, L. C. and Huang, S. C.: 1984, 'The Theory of a 2 MHz Resistivity Tool and its Application to Measurements-while-drilling', *The Log Analyst* **25**, 35–46.
- Cooper, R. K., Jackson, J. A., Burnett, L. J. and Harmon, J. F.: 1980, 'Remote (inside-out) NMR I. Remote Production of a Region of Homogeneous Magnetic Field, II. Sensitivity of NMR Detection for External Samples, and III. Detection of Nuclear Magnetic Resonance of a Remotely Produced Region of Homogeneous Magnetic Field', *J. Mag. Resonance* **41**, 400–421.
- Crone, J. D.: 1986, 'Field Examples of Borehole Pulse EM Surveys Used to Detect and Outline Conductive Ore Deposits', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85–27, pp. 59–70.
- Crone, J. D.: 1987, 'Case Histories of Borehole Pulse EM Surveys', *Minerals and Geotech. Logging Soc., 2nd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper K, pp. 133–138.
- Cryer, J., Dennis, B., Lewis, R. and Watfa, M.: 1987, 'Logging Techniques for Casing Corrosion', *The Technical Review* **35**, 32–38.
- Cull, J. P.: 1993, 'Downhole Three-component TEM Probes', *Explor. Geophys.* **24**, 437–442.
- Cull, J. P. and Cobcroft, R.: 1986, 'Omni-directional Downhole EM Probes', *Geophys. Prosp.* **34**, 569–579.
- Cuthbert, J. F. and Johnson, W. M., Jr.: 1974, 'New Casing Inspection Tool', *Soc. Petr. Eng. Conf.*, SPE 5090.
- Czubek, J. A.: 1971, 'Recent Russian and European Developments in Nuclear Geophysics Applied to Mineral Exploration and Mining', *The Log Analyst* **12**, 20–34.
- Daily, W., Lin, W. and Buschek, T.: 1987, 'Hydrological Properties of Topopah Spring Tuff: Laboratory Measurements', *J. Geophys. Res.* **92**, 7854–7864.
- Daily, W., Ramirez, A., LaBrecque, D. and Nitao, J.: 1992, 'Electrical Resistivity Tomography of Vadose Water Movement', *Water Resour. Research* **28**, 1429–1442.
- Daily, W. and Yorkey, T. J.: 1988, 'Evaluation of Cross-borehole Resistivity Tomography', *58th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, Session EM1.3.
- Daniels, J. J.: 1977, 'Three-dimensional Resistivity and Induced Polarization Modeling Using Buried Electrodes', *Geophysics* **42**, 1006–1019.

- Daniels, J. J.: 1978, 'Interpretation of Buried Electrode Resistivity Data Using a Layered Earth Model', *Geophysics* **43**, 988–1001.
- Daniels, J. J.: 1983, 'Hole-to-surface Resistivity Measurements', *Geophysics* **48**, 87–97.
- Daniels, J. J. and Dyck, A. F.: 1984, 'Borehole Resistivity and Electromagnetic Methods Applied to Mineral Exploration', *IEEE Trans. Geosci. Rem. Sens.* **GE-22**, 80–87.
- Davies, D. H., Faivre, O., Gounet, M.-T., Seeman, B., Troiller, J.-C., Benimeli, D., Ferreira, A. E., Pittman, D. J., Smits, J.-W., Randrianavony, M., Anderson, B. I. and Lovell, J.: 1992, 'Azimuthal Resistivity Imaging: A New Generation Lateralog', *Soc. Petrol. Engin. SPE 24676* Ω , 143–153.
- Dennis, B., Standen, E., Georgi, D. T. and Callow, G. O.: 1987, 'Fracture Identification and Productivity Prediction in a Carbonate Reef Complex', *Soc. Petr. Eng., SPE 16808*, pp. 579–588.
- DeSimone, L. A. and Barlow, P. M.: 1993, 'Borehole Induction Logging for Delineation of a Seepage-effluent Contaminant Plume in Glacial Outwash, Cape Cod, Massachusetts', *Minerals and Geotech. Logging Soc., 5th Intern. Symp. on Geophysics for Minerals, Geotech. and Environmental Applications, Proc., Soc. Prof. Well Log Anal.*, paper X, pp. 1–13.
- Dijkstra, A. M., Brown, B. H., Leathard, A. D., Harris, N. D., Barber, D. C. and Edbrooke, D. L.: 1993, 'Review: Clinical Applications of Electrical Impedance Tomography', *J. Med. Eng. Tech.* **17**, 89–98.
- Dines, K. A. and Lytle, R. J.: 1979, 'Computerized Geophysical Tomography', *Proc. IEEE* **67**, 1065–1073.
- Dines, K. A. and Lytle, R. J.: 1981, 'Analysis of Electrical Conductivity Imaging', *Geophysics* **46**, 1025–1036.
- Doe, A. R. D., Carsell, J. T., Smith, C. K., and Erickson, M. E.: 1991, 'Underground Downhole geophysics at the CSA Mine, Cobar, Australia – A Case Study', *Minerals and Geotech. Logging Soc., 4th Intern. Symp. on Borehole Geophysics for Minerals, Geotech. and Groundwater Applications, Proc., Soc. Prof. Well Log Anal.* pp. 143–148.
- Doll, G. H.: 1948, 'The SP Log: Theoretical Analysis and Principles of Interpretation', *Trans. AIME* **179**, Tech. Paper 2463.
- Doll, H. G.: 1949, 'Introduction to Induction Logging and Application to Logging of Wells Drilled With Oil-based Mud', *J. Petrol. Technol.* **1**, 148–162.
- Doll, H. G.: 1950, 'The Microlog: A New Electrical Logging Method for the Detailed Determination of Permeable Beds', *Petrol. Trans. AIME*.
- Doll, H. G.: 1951, 'The Laterolog: A New Resistivity Logging Method with Electrodes Using an Automated Focussing System', *Petrol. Trans. AIME* **192**, 305–316.
- Doll, H. G., Dumanoir, J. L., and Martin, M.: 1960, 'Suggestions for Better Electric Log Combinations and Improved Interpretations', *Geophysics* **25**, 854–882.
- Draxler, J. K., Lingnau, R., and Wöhrl, T.: 1990, 'Formation Microscanner Application in Crystalline Rocks', *13th SPWLA European Formation Evaluation Symp., October 1990, Budapest, SPWLA paper KK*, pp. 1–19.
- Duncan, A. C. and Cull, J. P.: 1988, 'Three-component Downhole TEM Surveys', *Expl. Geophys.* **19**, 51–53.
- Dyck, A. V. (ed.): 1975, *Borehole Geophysics Applied to Metallic Mineral Prospecting: A Review*, Dept. of Energy, Mines and Resources, Geological Survey of Canada, Paper 75–31, Ottawa.
- Dyck, A. V.: 1991, 'Drill-hole Electromagnetic Methods', in M. N. Nabighian (ed.), *Electromagnetic Methods in Applied Geophysics*, Soc. Expl. Geophys., Tulsa, pp. 881–930.
- Dyck, A. V. and Asten, M. W.: 1988, 'Electromagnetic Exploration from Boreholes', in G. D. Garland (ed.), *Proceedings of Exploration '87*, Ontario Geological Survey, pp. 122–136.
- Dyck, A. V. and Young, R. P.: 1985, 'Physical Characterization of Rock Masses Using Borehole Methods', *Geophysics* **50**, 2530–2541.
- Eadie, T.: 1987, 'The Downhole EM Response of the Hellyer Ore Deposit', *Expl. Geophys.* **18**, 255–264.
- Eadie, E. T. and Staltari, G. (eds.): 1987, *Downhole Electromagnetic Methods*: Special issue of *Explor. Geophys.*, **18**, no. 3, 107 pp., Austr. Soc. Expl. Geophys..
- Eadie, T. and Staltari, G.: 1987, 'Introduction to Downhole Electromagnetic Methods', *Expl. Geophys.* **18**, 247–254.

- Edwards, R. N.: 1988, 'A Down-hole Magnetometric Resistivity Technique for Electrical Sounding Beneath a Conductive Surface Layer', *Geophysics* **53**, 528–538.
- Edwards, R. N. and Howell, E. C.: 1976, 'Field Test of the Magnetometric Resistivity (MMR) Method', *Geophysics* **41**, 1170–1183.
- Ekstrom, M. P., Dahan, C. A., Chen, M., Lloyd, P. M., and Rossi, D. J.: 1986, 'Formation Imaging With Microelectrical Scanning Arrays', *27th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper BB.
- Elliott, C. L.: 1961, 'An Electromagnetic Drill Hole Instrument for the Detection of Conductive Sulfide Ore Bodies (abstract only)', *Geophysics* **26**.
- Ellis, D. V.: 1987, *Well Logging for Earth Scientists*, Elsevier.
- Emilsson, J. and Wanstedt, S.: 1993, 'Geophysical Multiparameter Logging Techniques Applied to Ore Exploration in the Skellefte Field', *Minerals and Geotech. Logging Soc., 5th Intern. Symp. on Geophysics for Minerals, Geotech. and Environmental Applications, Proc.*, Soc. Prof. Well Log Anal., paper Q, pp. 1–7.
- Fox, R. W.: 1830, 'On the Electro-magnetic Properties of Metalliferous Veins in the Mines of Cornwall', *Roy. Soc. London Philos. Trans.*, pt. 2 **120**, 399–414.
- Frignet, B., 1986, 'Induction Logs Applied to Mineral Exploration and Development', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85-27, pp. 89–100.
- Fuller, B. D. and Ward, S. H.: 1970, 'Linear System Description of the Electrical Properties of Rocks', *IEEE Trans. Geosci. Electron.* **GE-8**, 7–18.
- Gasnier, S., Shima, H., Sakashita, S. and Abdelhadi, A.: 1994, 'Development of Multi-component Multi-frequency Data Acquisition System for Borehole EM Tomography', *56th Mtg. Eur. Assoc. Expl Geophys., Abstracts*, paper I030.
- Gish, O. H.: 1923, 'General Description of the Earth-current Measuring System at the Watheroo Magnetic Observatory', *Terr. Magn. Atmos. Elec.* **28**, 89–108.
- Glenn, W. E. and Nelson, P. H.: 1979, 'Borehole Techniques Applied to Base Metal Ore Deposits', in P. J. Hood (ed.), *Geophysics and Geochemistry in the Search for Metallic Ores*, Geol. Surv. Canada, Econ. Report 31, Ottawa, pp. 273–294.
- Goldman, M.: 1990, *Non-conventional Methods in Geoelectrical Prospecting*, Ellis Horwood.
- Gondouin, M. and Scala, C.: 1958, 'Streaming Potential and the SP Log', *Trans. AIME*, Tech. Paper 8023.
- Grant, F. S. and West, G. F.: 1965, *Interpretation Theory in Applied Geophysics*, McGraw-Hill Book Co.
- Grinat, M.: 1991, 'First Experiences With a New Induced Polarization Tool in the KTB-Oberpfalz VB', *Scientific Drilling* **2**, 160–165.
- Haak, V., Stoll, J., and Winter, H.: 1991, 'Why is the Electrical Resistivity Around the KTB Hole so Low?', *Phys. Earth Planet. Inter.* **66**, 12–23.
- Halleux, L., Feller, P., Monjoie, A., and Pissart, R.: 1992, 'Ground Penetrating and Borehole Radar Surveys in the Borth Salt Mine (FRG)', *Fourth Int. Conf. on Ground Penetr. Radar*, Geol. Surv. Finland, Special Paper 16, pp. 317–321.
- Hamilton, R. G.: 1960, 'Application of the Proximity Log', *1st Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper 6.
- Hearst, J. R. and Nelson, P. H.: 1985, *Well Logging for Physical Properties*, McGraw-Hill.
- Henderson, R. P. and Brown, B. H.: 1984, 'Review Article: Applied Potential Tomography', *J. Phys. Sci. Instru.* **17**, 723–733.
- Hill, D. A.: 1984, 'Radio Propagation in a Coal Seam and the Inverse Problem', *J. Res. National Bur. Standards (USA)* **89**, 385–394.
- Hishida, H., Minama, H., and Tsujimoto, T., 1992, 'Case Study of Resistivity Tomography in Mining Districts', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 229–247.
- Hodges, D. G., Crone, J. D., and Pemberton, R.: 1991, 'A New Multiple Component Downhole Pulse EM Probe for Directional Interpretation', *Minerals and Geotech. Logging Soc., 4th Intern. Symp. on Borehole Geophysics for Minerals, Geotech. and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., pp. 107–123.

- Hohmann, G. W., van Voorhis, G. D., and Nelson, P. H.: 1978, 'A Vector EM System and its Field Applications', *Geophysics* **43**, 1418–1440.
- Holloway, A. L., Stevens, K. M. and Lodha, G. S.: 1992, 'The Results from Surface and Borehole Radar Profiling from Permit Area B of the Whiteshell Research Area, Manitoba, Canada', *Fourth Int. Conf. on Ground Penetr. Radar*, Geol. Surv. Finland, Special Paper 16, pp. 329–337.
- Hollyer, G. M., Wilherly, K. E., V., D. A., Diorio, P. A., and Golden, H. C.: 1991, 'Physical Property Log in Applied to Base Metal and Gold Exploration', *Minerals and Geotech. Logging Soc., 4th Intern. Symp. on Borehole Geophysics for Minerals, Geotech. and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., pp. 419–427.
- Holser, W. T., Brown, R. J. S., Roberts, F. A., Fredriksson, O. A., and Unterberger, R. R.: 1972, 'Radar Logging of a Salt Dome', *Geophysics* **37**, 889–906. See also Discussion in *Geophysics* **38**, 981.
- Hornby, B. E., Luthi, S. M., and Plumb, R. A.: 1992, 'Comparison of Fracture Apertures Computed from Electrical Borehole Scans and Reflected Stoneley Waves: An Integrated Interpretation', *The Log Analyst* **33**, 50–66.
- Hoyer, D. L.: 1991, 'Evaluation of Coalbed Fracture Porosity from Dual Laterolog', *The Log Analyst* **32**, 654–662.
- Hull, P. W. and Coolidge, J. E.: 1960, 'Field Results With Nuclear Magnetism Logging', *1st Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper 11.
- Irvine, R. J.: 1987, 'Drillhole TEM Surveys at Thalanga, Queensland', *Expl. Geophys.* **18**, 285–293.
- Iseki, S.-i. and Shima, H.: 1992, 'Induced Polarization Tomography: A Cross-hole Imaging Technique Using Chargeability and Resistivity', *62nd Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 439–442.
- Jackson, J. and Matthews, M.: 1993, 'Nuclear Magnetic Resonance Bibliography', *The Log Analyst* **34**, 35–69.
- Jakosky, J. J.: 1933, *Method and Apparatus for Determining Underground Structure*, US Patent No. 1906271.
- Jakosky, J. J.: 1940, *Geophysical Prospecting*, Times-Mirror Press, Los Angeles.
- Jiajin, L. and Harvey, A. H.: 1982, 'Coal Logging in the People's Republic of China', *The Log Analyst* **23**, 3–8.
- Johnson, H. M.: 1962, 'A History of Well-logging', *Geophysics* **27**, 507–527.
- Jorden, J. R. and Campbell, F. L.: 1986, *Well Logging II - Electric and Acoustic Logging*, Soc. Petr. Eng., Monogr., vol 10., New York.
- Kaufman, A. A.: 1990, 'The Electrical Field in a Borehole With a Casing', *Geophysics* **55**, 29–38.
- Kaufman, A. A. and Wightman, W. E.: 1993, 'A Transmission Line for Electrical Logging Through Casing', *Geophysics* **58**, 1739–1747.
- Kayal, J. R. and Chistoffel, D. A.: 1989, 'Coal Quality from Geophysical Logs; Southland Lignite Region, New Zealand', *The Log Analyst* **30**, 343–352.
- Keller, G. V. and Frischknecht, F. C.: 1966, *Electrical Methods of Geophysical Prospecting*, Pergamon Press.
- Kelly, S. F.: 1950, 'The Rise of Geophysics', *Can. Mining Manual*, pp. 1–7.
- Killeen, P. G. and Mwenifumbo, C. J.: 1987, 'Interpretation of New Generation Geophysical Logs in Canadian Mineral Exploration', *Minerals and Geotech. Logging Soc., 2nd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper N, pp. 167–178.
- Killeen, P. G. (ed.): 1985, *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can., Paper 85-27.
- Klein, J. D. and Martin, P. R.: 1993, 'Cement Resistivity and Implications for Measurement of Formation Resistivity Through Casing', *68th Ann. Tech. Conf., Soc. Petr. Eng., SPE 26453*, pp. 365–380.
- Kobr, M.: 1990, 'Borehole and Petrophysics Investigations Applied to Metallic Mineral Prospecting in the Zlate Hory Ore District, NW Moravia, Czechoslovakia', *13th European Formation Evaluation Symp. Trans., Budapest Chapter*, Soc. Prof. Well Log Anal., paper SS, pp. 1–11.

- Koepsell, R. J., Jensen, F. E., and Langley, R. L.: 1989, 'Gulf Coast Fault Orientation Determined by Formation Imaging Techniques', *30th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper VV, pp. 1–25.
- Kong, F. N., Westerdahl, H. and By, T. L.: 1993, 'Borehole Radar Tunnel Detection at Gjøvik, Norway', *Fourth Tunnel Detection Symp. on Subsurf. Explor. Technology*, U.S. Government Printing Office 1993-363-415. pp. 649–658.
- Kretzschmar, J. L., Kibbe, K. L., and Witterholt, E. J.: 1982, 'Tomographic Reconstruction Techniques for Reservoir Monitoring', *57th SPE Ann. Fall Conf.*, SPE 10990.
- Kück, J.: 1992, 'A Comparison of Electrical Resistivities Obtained from Logging the KTB Pilot Hole With Surface Electromagnetic Measurements', *Scientific Drilling* **3**, 100–104.
- Kunetz, G.: 1966, *Principals of Direct Current Resistivity Prospecting*, Gebruder Borntraeger, Berlin.
- Labert, F.: 1981, 'Logging for Mineral Exploration (in French)', *7th European Formation Evaluation Symp. Trans., Paris Chapter (SAID)*, Soc. of Prof. Well Log Anal., paper 29.
- Labo, J.: 1987, *A Practical Guide to Borehole Geophysics: An Overview of Wireline Well Logging Principles for Geophysicists*, Soc. Expl. Geophys., Tulsa.
- LaBrecque, D. J.: 1991, 'IP tomography', *61st Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 413–416.
- Lager, D. L. and Lytle, R. J.: 1977, 'Determining a Subsurface Electromagnetic Profile from High Frequency Measurements by Applying Reconstruction-technique Algorithms', *Radio Science* **12**, 249–260.
- Lane, R. J. L.: 1987, 'The Downhole EM Response of an Intersected Massive Sulphide Deposit, South Australia', *Expl. Geophys* **18**, 313-318.
- Laubach, S. E., Baumgardner, R. W., Jr., Monson, E. R., Hunt, E., and Meador, K. J.: 1988, 'Fracture Detection in Low Permeability Reservoir Sandstone: A Comparison of BHTV and FMS Logs to Core', *SPE Ann. Conf., SPE 18119* Ω , pp. 129–139.
- Le Masne, D. and Poirmeur, C.: 1988, 'Three-dimensional Model Results for an Electrical Hole-to-surface Method – Application to the Interpretation of a Field Survey', *Geophysics* **53**, 85–103.
- Lee, J.: 1986, *A Three-component Drillhole EM Probe*, M.Sc. Thesis, Univ. of Toronto.
- Levy, G. M. and McNeill, J. D.: 1986, 'Transient Electromagnetic Borehole Logging', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85-27, pp. 71–78.
- Lo, B. B. H. and Edwards, R. N.: 1986, 'Design and Field Tests of a Sensor for the Crosshole Magnetometric Resistivity Technique', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Canada, Paper 85-27, pp. 289–296.
- Luthi, S. M. and Banavar, J. R.: 1988, 'Application of Borehole Images to Three-dimensional Geometric Modeling of Eolian Sandstone Reservoirs, Permian Rotliegende, North Sea', *AAPG Bull.* **72**, 1074–1089.
- Luthi, S. M. and Souhaité, P.: 1990, 'Fracture Apertures from Electrical Borehole Scans', *Geophysics* **55**, 821–833.
- Lytle, R. J. and Dines, K. A.: 1978, 'An Impedance Camera: A System for Determining the Spatial Variation of Electrical Conductivity', *Lawrence Livermore Laboratory, Livermore, California*, Report UCRL- 52413.
- Lytle, R. J. and Dines, K. A.: 1980, 'Iterative Ray Tracing Between Boreholes for Underground Image Reconstruction', *IEEE Trans. Geosci. Rem. Sens.* **GE-18**, 234–240.
- Lytle, R. J., Laine, E. F., Lager, E. F., and Davis, D. T.: 1979, 'Cross-borehole Electromagnetic Probing to Locate High-contrast Anomalies', *Geophysics* **44**, 1667–1676.
- Madden, T. R. and Cantwell, T.: 1967, 'Induced-polarization - A Review', in S. M. Comm. (ed.), *Mining Geophysics*, Soc. Expl. Geophys., Tulsa, pp. 373–400.
- Mahrer, K. D. and List, D. F.: 1995, 'Radio Frequency Electromagnetic Tunnel Detection and Delineation at the Otay Mesa Site', *Geophysics* **60**, 413–422.
- Martin, D. W., Spencer, M. C., and Patel, H.: 1984, 'The Digital Induction - A New Approach in the Response of the Induction Measurement', *25th Annual Logging Symposium Transactions*, Society of Professional Well Log Analysts paper M, pp. 1–11.
- Maltezos, F. and Anderson, R. N.: 1991, 'Milankovitch Cycles in Electrical Resistivity Logs from the Toa Baja Scientific Drillhole, Puerto Rico', *Geophys. Res. Letters* **18**, 517–520.

- Mathisrud, G. C. and Sumner, J. S.: 1967, 'Underground IP Survey at Homestead Mine', *Min. Congress J.* **53**, 66–69.
- Matteucci, M. C.: 1865, 'Sur les Courants Electriques de la Terre (on the Electric Currents of the Earth)', *Annales Chimie et Physique*, ser 4, **4**, 177–192.
- Mauchly, S. J.: 1918, 'A Study of Pressure and Temperature Effects in Earth-current Measurements', *Terr. Magn. Atmos. Elec.* **23**, 73–91.
- Maute, R. E.: 1992, 'Electrical Logging: State-of-the-art', *The Log Analyst* **33**, 206–227.
- McCollum, B. and Logan, K. H.: 1913, 'Electrolytic Corrosion of Iron in Soils', *U.S. Bur. Standards tech. Publ.* **25**, 69 pp.
- McGann, G. J., Riches, H. A., and Renoult, D. C.: 1988, 'Formation Evaluation in a Thinly Bedded Reservoir, a Case History: Scapa Field, North Sea', *29th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper V, pp. 1–20.
- McGaughey, W. J.: 1991, 'Crosshole Frequency-domain EM in Mineral Exploration', *Proc. 4th Inter. Symp. Borehole Geophys. Miner. Geotech. Groundw. Applic.*, Soc. Petr. Well Log Anal. 36–37.
- McMurray, H. V. and Hoagland, A. D.: 1956, 'Three Dimensional Applied Potential Studies at Austinville, Virginia', *Bull. Geol. Soc. Am.* **67**, 683–696.
- Miller, M. N., Paltiel, Z., Gillen, M. E., Granot, J. and Bouton, J. C.: 1990, 'Spin Echo Magnetic Resonance Logging: Porosity and Free Fluid Index Determination', *Soc. Petrol. Eng., SPE 20561* Ω , pp. 321–334.
- MGLS.: 1987, 'Proceedings of the Second International Symposium on Borehole Geophysics for Minerals, Geotechnical, and Goundwater Applications', *Minerals and Geotech. Logging Soc.*, Soc. Petrol. Well Log Anal.
- MGLS.: 1989, 'Proceedings of the Third International Symposium on Borehole Geophysics for Minerals, Geotechnical, and Goundwater Applications', *Minerals and Geotech. Logging Soc.*, Soc. Petrol. Well Log Anal.
- MGLS.: 1991, 'Proceedings of the Fourth International Symposium on Borehole Geophysics for Minerals, Geotechnical, and Goundwater Applications', *Minerals and Geotech. Logging Soc.*, Soc. Petrol. Well Log Anal.
- MGLS.: 1993, 'Proceedings of the Fifth International Symposium on Borehole Geophysics for Minerals, Geotechnical, and Goundwater Applications', *Minerals and Geotech. Logging Soc.*, Soc. Petrol. Well Log Anal.
- Monrose, H. and Boyer, S.: 1992, 'Casing Corrosion – Origin and Detection', *The Log Analyst* **33**, 507–519.
- Moran, M. L. and Greenfield, R. J.: 1993, 'Radar Signature of 2.5-D tunnel', *Geophysics* **58**, 1573–1587.
- Morriss, C. E., MacInnis, J., Freedman, R., Smaardyk, J., Straley, C., Kenyon, W. E., Vinegar, H. J., and Tutunjian, P. N.: 1993, 'Field Test of an Experimental Pulsed Nuclear Magnetism Tool', *34th Ann. Logging Symp. Transactions*, Soc. Prof. Well Log Anal., paper GGG, pp. 1–23.
- Mullins, O., Mitra-Kirtley, S. and Zhu, Y.: 1992, 'The Electronic Absorption Edge of Petroleum', *Appl. Spectrosc.* **46**, 1505–1411.
- Mutton, A. J.: 1987, 'Applications of Downhole SIROTEM Surveys in the Agnew Nickel Belt, W.A.', *Expl. Geophys.* **18**, 295–303.
- Mwenifumbo, C. J., 1986, 'Drillhole Mise-à-la-masse Induced Polarization and Potential Measurements in a Zn-Pb-Cu Sulphide Deposit', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotech. Applications*, Geol. Surv. Can. Paper 85-27, pp. 145–158.
- Mwenifumbo, C. J.: 1987, 'Cross-borehole Mise-à-la-masse Mapping of Fracture Zones at the Bells Corners Borehole Geophysical Test Area, Ottawa, Canada', *Minerals and Geotech. Logging Soc., 2nd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper M, pp. 151–165.
- Mwenifumbo, C. J.: 1989, 'Optimization of Logging Parameters in Continuous Time-domain Induced Polarization Measurements', *Minerals and Geotech. Logging Soc., 3rd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper N, pp. 201–232.
- Nabighian, M. N.: 1984, 'Foreword and Introduction – Time-domain Electromagnetic Methods of Exploration', *Geophysics* **49**, 849–853.

- Nabighian, M. N., Oppliger, G. L., Edwards, R. N., Lo, B. B. H., and Chessman, S. J.: 1984, 'Cross-hole Magnetometric Resistivity', *Geophysics* **49**, 1313–1326.
- Nekut, A. G.: 1994, 'Electromagnetic Raytrace Tomography', *Geophysics* **59**, 371–377.
- Nekut, A. G.: 1995, 'Crosswell Electromagnetic Tomography in Steel Cased Wells', *Geophysics* **60**, 912–920.
- Newman, G. A.: 1995, 'Crosswell Electromagnetic Inversion Using Integral and Differential Equations', *Geophysics* **60**, 899–911.
- Nickel, H., Sender, F., Thierbach, R., and Weichart, H.: 1983, 'Exploring the Interior of Salt-domes from Boreholes', *Geophys. Prosp.* **31**, 131–148.
- Nilsson, B., 1986, 'A New Borehole Radar System', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotech. Applications*, Geol. Surv. Can. Paper 85-27, pp. 189–196.
- Noakes, J.: 1951, *An Electromagnetic Method of Geophysical Prospecting for Application to Drill Holes*. Ph. D. Thesis, Univ. of Toronto.
- Ogilvy, R. D.: 1983, 'Application of Down-hole Pulse Electromagnetic Surveys for Off-hole Mineral Exploration', *Trans. Instn Min. Metall. (Sect. B: Appl. Earth Sci.)* **92**, B148–B153.
- Ogilvy, R. D.: 1985a, 'Down-hole IP Applied to Off-hole Mineral Exploration – Some Design Consideration', *Geoexploration* **22**, 59–73.
- Ogilvy, R. D.: 1985b, 'Down-hole IP/resistivity Prospecting in Mineral Drill-holes – Some Illustrative Field Examples', *Geoexploration* **22**, 257–273.
- Okada, J. T., Laine, E. F., Lytle, R. J. and Dailey, W. D.: 1980, 'Geotomography Applied to the Stripa Mine in Sweden', *Lawrence Livermore Nat. Lab.*, UCRL-52961.
- Olhoeft, G. R.: 1988, 'Interpretation of Hole-to-hole Radar Measurements', *Third Technical Symp. on Tunnel Detection, Proc.*, U. S. Government Printing Office pp. 126–141.
- Olsson, B. and Nilsson, B., 1986, 'Some Examples from Borehole Radar Measurements', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85-27, pp. 197–206.
- Olsson, O., Falk, L., Forslund, O., Lundmark, L. and Sandberg, E.: 1992, 'Borehole Radar Applied to the Characterization of Hydraulically Conductive Fracture Zones in Crystalline Rock', *Geophysical Prospecting* **40**, 109–142.
- Olsson, O., Falk, L., Forslund, O., Niva, B., and Sandberg, E.: 1989, 'Borehole Radar Applied to Characterization of Fracture Zones', *Exploration Geophysics* **2**, 149–152.
- Osato, K. and Takasugi, S., 1992, 'The Possibility of Subsurface Borehole Electromagnetic Surveys in Geothermal Reservoirs (Part 2) – Development of Borehole Tool and Field Test', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 343–360.
- Owen, J. E. and Greer, W. J.: 1951, 'The Guard Electrode System', *AIME*, Tech. Paper 3222.
- Paillet, F., Barton, C., Luthi, S., Rambow, F., and Zamanek, J. (eds.): 1990, *Borehole Imaging (Reprint series)*, Soc. Prof. Well Log. Anal., Tulsa, Oklahoma.
- Pantze, R., Malmqvist, L. and Kristensson, G., 1986, 'Directional EM Measurements in Boreholes', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Canada, Paper 85-27, pp. 79–88.
- Parasnis, D. S.: 1967, 'Three-dimensional Electric Mise-à-la-masse Survey of an Irregular Lead-zinc-copper Deposit in Central Sweden', *Geophys. Prosp.* **15**, 407–437.
- Pedersen, L. B., Juhlin, C. and Rasmussen, T. M.: 1992, 'Electric Resistivity in the Gravberg-1 Deep Well, Sweden', *J. Geophys. Res.* **97**, 9171–9182.
- Peeters, M. and Kempton, N. H.: 1977, 'Wireline Logging for Coal Exploration in Australia', *The Log Analyst* **18**, 24–29.
- Petrovsky, A. D.: 1971, *Radiovolnovye Metody v Podzemnoy Geofiziki (Underground Radio Wave Methods in Geophysics)*, Nedra, Moscow.
- Pezard, P. A.: 1992, 'Downhole Electrical Images in Volcanoclastic Sequences of the Izu-Bonin Forearc Basin, Western Pacific', *Proc. of the Ocean Drilling Program, Scientific Results*, **126**, 603–624.
- Pezard, P. A. and Luthi, S. M.: 1988, 'Borehole Electrical Images in the Basement of the Cajon Pass Scientific Drillhole, California; Fracture Identification and Tectonic Implications', *Geophys. Res. Letters* **15**, 1017–1020.

- Plumb, R. A. and Luthi, S. M.: 1986, 'Application of Borehole Images to Geologic Modeling of an Eolian Reservoir', *Soc. Petr. Eng. Conf, SPE 15487. Later published in SPE Formation Evaluation, 1988* 3(4), 505–514.
- Poirmeur, C.: 1987, 'Hole-to-hole Electrical Measurements: Mimafo Method', *Minerals and Geotech. Logging Soc., 2nd Intern. Symp. on Borehole Geophysics for Minerals, Geotech., and Groundwater Applications, Proc.*, Soc. Prof. Well Log Anal., paper X, pp. 265–271.
- Poley, J. P., Nootboom, J. J. and DeWaal, P. J.: 1978, 'Use of VHF Dielectric Measurements for Borehole Formation Analysis', *The Log Analyst* 19, 8–30.
- Prensky, S. E.: 1992, *Bibliography of Well-Log Applications, Cumulative Edition, to September 30, 1992*, U.S. Geological Survey Open-File Report OF 92-0390.
- Price, L. R.: 1979, 'Electrical Impedance Computer Tomography (ICT): A New CT Imaging Technique', *IEEE Trans. NS-26*, 2736–2739.
- Ramirez, A., Daily, W., LaBrecque, D., Owen, E. and Chesnut, D.: 1993, 'Monitoring an Underground Steam Injection Process Using Electrical Resistance Tomography', *Water Resour. Res.* 29, 73–87.
- Rauen, A., Duyster, J., Kontny, A. and Röckel, T.: 1994, 'Influence of Cracks and Ore Mineralization on the Electrical Conductivity: an Example from KTB', *VII Ann. Symp. on the Observ. of the Contin. Crust thr. Drilling*, Santa Fe, New Mexico, Apr. 25–28, 1994.
- Rauen, A. and Lastovickova, M.: 1995, 'Investigation of Electrical Anisotropy in the Deep Borehole KTB', *Surv. in Geophys.* 16, 37–46.
- Reed, L. E., 1986, 'A Borehole Electromagnetic Survey of the South Bay Mine, Ontario', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85-27, pp. 307–322.
- Reed, L. E.: 1993, 'Definition of Ore at Les Mines Selbaie Using Mise à la Masse', *The Log Analyst* 34, 26–34.
- Reeves, D. R.: 1972, 'Applications of Wireline Logging Techniques to Mineral Exploration', *1st European Formation Evaluation Symp. Trans., Paris Chapter (SAID)*, Soc. Prof. Well Log Anal., paper 5.
- Reeves, D. R.: 1976, 'Development of Slimline Logging Systems for Coal and Mineral Exploration', *17th Ann. Logging Symp. Trans.*, Soc. of Prof. Well Log Anal., paper KK, pp. 1–16.
- Richards, D. J.: 1987, 'CRAE's Approach to Downhole TEM at Broken Hill', *Expl. Geophys.* 18, 279–284.
- Robertson, K. A. and Ascough, G. L.: 1991, 'A Study of Borehole Time Domain Electromagnetic Surveys from the Heath Steele/stratmat Properties of Northern New Brunswick', *Minerals and Geotech. Logging Soc., 4th Intern. Symp. on Borehole Geophysics for Minerals, Geotech. and Groundwater Applications, Proc.*, Soc. of Prof. Well Log Anal. 125–142.
- Rocroi, J. P. and Koulikov, A. V.: 1985, 'The Use of Vertical-line Sources in Electrical Prospecting for Hydrocarbon', *Geophys. Prosp.* 33, 138–154.
- Rodney, P. F., Wisler, M. M., Thompson, L. W., and Meador, R. A.: 1983, 'The Electromagnetic Wave Resistivity MWD tool', *58th Ann. Conf. Soc. Petr. Engin.*, SPE 12167, 16 pp.
- Rogers, G., Brandt, L., Young, J., and Kot, J.: 1993, 'The Study of Diffusion Effects in RIM Tomographic Imaging', *Explor. Geophys.* 24, 785–788.
- Rogers, P. G., Edwards, S. A., Young, J. A., and Downey, M.: 1987, 'Geotomography for the Delineation of Coal structure', *Geoexploration* 24, 301–328.
- Runge, R. J., Worthington, A. E. and Lucas, D. R.: 1969, 'Ultra-Long Spaced Electric Log (ULSEL)', *10th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper H, pp. 1–22.
- Rust, W. M. J.: 1938, 'A Historical View of Electrical Prospecting Methods', *Geophysics* 3, 1–6.
- Rust, W. M. J.: 1940, 'Typical Electrical Prospecting Methods', *Geophysics* 5, 243–249.
- Sakashita, S. and Shima, H.: 1993, 'Controlled Source Magnetic Susceptibility Tomography', *63rd Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, 377–380.
- Sakashita, S., Shima, H. and Gasnier, S.: 1994, 'Controlled Source EM Tomography: an Improved Imaging Technique for Magnetic Susceptibility and Resistivity', *56th Mtg. Eur. Assoc. Expl. Geophys., Abstracts*, paper 1029.
- Salt, D. J., 1966, 'Tests of Drill-hole Methods of Geophysical Prospecting on the Property of Lake Dufault Mines Limited Dufresnoy Township Quebec', in S. M. Comm. (ed.), *Mining Geophysics*, Soc. Expl. Geophys., Tulsa, pp. 206–226.

- Sandberg, E. V., Olsson, O. L. and Falk, L. R.: 1991, 'Combined Interpretation of Fracture Zones in Crystalline Rock Using Single-hole and Crosshole Tomography and Directional Borehole-radar Data', *The Log Analyst* **32**, 104–115.
- Sasaki, Y.: 1994, 'Anisotropic Resistivity Tomography: A Model Study for Characterization of Fractured Rocks', *56th Mtg. Eur. Assoc. Expl. Geophys., Abstracts*.
- Sasaki, Y. and Matsuo, K.: 1990, 'Surface-to-tunnel Resistivity Tomography at a Copper Mine', *60th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 550–553.
- Sasaki, Y., Matsuo, K. and Yokoi, K.: 1994, 'Resistivity Inversion of Cross-hole and Borehole-to-surface EM Data Using Axially Symmetric Models', *Geophys. Prosp.* **42**, 745–754.
- Schenkel, C. J. and Morrison, H. F.: 1994, 'Electrical Resistivity Through Metal Casing', *Geophysics* **59**, 1072–1082.
- Schlumberger, C.: 1920, *Étude Sur la Prospection Électrique du Sous-sol*, Gauthier-Villars et Cie, Paris.
- Schlumberger, C., Schlumberger, M. and Leonardon, E. G.: 1932, 'Electrical Coring: A Method of Determining Bottom-hole Data by Electrical Measurements', *Am. Inst. Min. Eng. Tech. Pub.* 462.
- Schlumberger, C., Schlumberger, M. and Leonardon, E. G.: 1933, 'A New Contribution to Subsurface Studies by Means of Electrical Measurements in Drill Holes', *Am. Inst. Min. Eng., Tech. Pub.* 503 (also in 1934, *Trans.* **110**, 159–182).
- Schoen, J. H.: 1993, 'Hydrogeological Information for Water Exploration and Environmental Investigation from Well Log Measurements', *Minerals and Geotech. Logging Soc., 5th Intern. Symp. on Geophysics for Minerals, Geotech. and Environmental Applications, Proc., Soc. Prof. Well Log Anal.*, paper F, pp. 1–8.
- Scott, J. H., Seeley, R. L. and Barth, J. J.: 1981, 'A Magnetic Susceptibility Well-logging System for Mineral Exploration', *22nd Ann. Logging Symp. Trans., Soc. Prof. Well Log Anal.*, paper CC, pp. 1–21.
- Segesman, F. F.: 1980, 'History of Geophysical Exploration – Well-logging Method', *Geophysics* **45**, 1667–1684.
- Sen, P. N.: 1991, 'Correspondence Between Membrane Potential and Conductivity', *Geophysics* **56**, 461–471.
- Sen, P. N., Scala, C. and Cohen, M. H.: 1981, 'A Self-similar Model for Sedimentary Rocks With Application to the Dielectric Constant of Fused Glass Beads', *Geophysics* **46**, 781–795.
- Sena, A. G. and Toksoz, M. N.: 1990, 'Simultaneous Reconstruction of Permittivity and Conductivity for Crosshole Geometries', *Geophysics* **55**, 1302–1311.
- Serra, O.: 1984, *Fundamentals of Well-log Interpretation, Vol 1. The Acquisition of Logging Data*, Elsevier.
- Serra, O.: 1986, *Fundamentals of Well-Log Interpretation, Vol 2. The Interpretation of Logging Data*, Elsevier.
- Shibamoto, M., Moriyama, K., Yamamoto, M., and Noguchi, K., 1992, 'Application of Resistivity Tomography for Prospecting Grouting Zone in Sandy Ground', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 209–228.
- Shima, H.: 1992a, '2-D and 3-D Resistivity Image Reconstruction Using Crosshole Data', *Geophysics* **57**, 1270–1281.
- Shima, H.: 1992b, 'Vertical Electric Imaging: A New Technique to Image Electric Reflectivity Near Borehole', *54th Mtg. Eur. Assoc. Expl. Geophys., Abstracts*, pp. 360–361.
- Shima, H.: 1993, 'Vertical Electrical Imaging Using Focused Current and Its Application', *55th Mtg. Eur. Assoc. Expl. Geophys., Abstracts*, Session D033.
- Shima, H. and Saito, H.: 1988, 'Application of Resistivity Tomography for Detection of Faults and Evaluation of Their Hydraulic Continuity: Some Numerical Experiments', *58th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, Session EM1.4.
- Shima, H. and Sakayama, T.: 1987, 'Resistivity Tomography: An Approach to 2-D Resistivity Inverse Problems', *57th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, Session:EM1.4.
- Shope, S. M., Greenfield, R. J. and Stolarczrk, L.: 1986, 'Use of Electromagnetic Waves for longwall Coal Seam Tomography', *56th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, Session EM3.4.

- Smith, G.: 1981, 'Principle and application of New Method for Inspection of Well Casing', *Soc. Petr. Eng. Conf.*, SPE 9630.
- Smith, R. J. and Hallof, P. G.: 1971, 'A New Deep Drill-hole Electromagnetic System (abstract only)', *Geophysics* **36**, 1280.
- Smits, A. R., Fincher, D. V., Nishida, K., Mullins, O. C., Schroeder, R. J., and Yamate, T.: 1993, 'In-situ Fluid Analysis as an Aid to Wireline Formation Sampling', *68th Ann. Conf., Soc. Petrol. Eng.*, SPE 26496.
- Spies, B. R.: 1992, 'Survey Design Considerations for Cross-well Electromagnetics', *62nd Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 498–501.
- Spies, B. R. and Greaves, R. J.: 1991, 'Numerical Modeling of Surface-to-borehole Electromagnetic Surveys for Monitoring Thermal Enhanced oil Recovery', *Geoexploration* **28**, 293–311.
- Spies, B. R. and Ellis, R. G.: 1995, 'Cross-borehole Resistivity Tomography of a Pilot-scale In-situ Vitrification Test', *Geophysics* **60**, 886–898.
- Spies, B. R. and Habashy, T. M.: 1995, 'Sensitivity Analysis of Crosswell Electromagnetics', *Geophysics* **60**, 834–845.
- Spitzer, K.: 1993, 'Observations of Geomagnetic Pulsations and Variations with a New Borehole Magnetometer Down to Depths of 3000 m.', *Geophys. J. Int.* **115**, 839–848.
- SPWLA.: 1992, *SPWLA Reprint Volume: Resistivity Logging*, Soc. Prof. Well Log. Anal., Tulsa, Oklahoma.
- SPWLA.: 1985, *Index to Well Logging Literature, 1965–1984*, Univ. Tulsa Inform. Services Division, and Tulsa Chapter of S.P.W.L.A, Tulsa, Oklahoma.
- Stefanescu, S.: 1970, 'Nouvelles Applications de la Théorie des Milieux Alpha Harmoniques à la Prospection électrique en Courant Continu', *Geophys. Prosp.* **18**, 786–799.
- Steveling, E., Spitzer, K. And Leven, M.: 1991, 'Vertical Gradient of Horizontal Geomagnetic Variations – First Results With the Göttingen Borehole Magnetometer in the KTB-Oberpfalz VB', *Scientific Drilling* **2**, 180–187.
- Stewart, R. D. and Unterberger, R. R.: 1976, 'Seeing Through Rock-salt With Radar', *Geophysics* **41**, 123–132.
- Stolarczyk, L. and Fry, R. C.: 1989, 'Radio Imaging Method (RIM) or Diagnostic Imaging of Anomalous Geologic Structures in Coal Seam Waveguides', *Trans. Soc. Min. Metall. and Explor.* **288**, 1806–1814.
- Stolarczyk, L., Rogers, G. and Hatherly, P.: 1988, 'Comparison of Radio Imaging Method (RIM-I) Electromagnetic Wave Tomography With in-mine Geological Mapping in the Lidell, Bulli and Wongawilli Coal Seams', *Explor. Geophys.* **19**, 169–170.
- Stolarczyk, L. G.: 1990, 'Radio Imaging in Seam Waveguides', in S. H. Ward (ed.), *Geotechnical and Environmental Geophysics*, Soc. Expl. Geophys., Tulsa, pp. 187–209.
- Stoll, J.: 1993, 'A Mise-à-la Masse Experiment for Detecting an Electric Network in Cataclastic Zones Around KTB-site', in K. Bram and J. K. Draxler (ed.), *KTB Report 93-1; Basic Research and Borehole Geophysics (Report 14)*, Projektgruppe Kontinentales Tiefbohrprogramm der Bundesrepublik Deutschland am Niedersächsischen Landesamt für Bodenforschung, Stuttgart, Germany, pp. 237–250.
- Stoll, J.: 1994, 'On the Dynamic Behavior of Local SP-amplitudes During a Hydraulic Pump Test in the KTB', *VII Ann. Symp. on the Observ. of the Contin. Crust thr. Drilling*, Santa Fe, New Mexico, Apr. 25–28, 1994.
- Straub, A., Kruckel, U., and Gros, Y.: 1991, 'Borehole Electrical Imaging and Structural Analysis in a Granitic Environment', *Geophysical Journal Intern.* **106**, 635–646.
- Straub, A. and Valla, P.: 1987, 'Applications of Induction Tools in Borehole Geophysics', *Proc. 2nd Inter. Symp. Borehole Geophys. Miner. Geotech. Groundw. Applic.*, Soc. Petr. Well Log Anal., Paper XX.
- Suau, J., Grimaldi, P., Poupon, A. and Souhaite, P.: 1972, 'The Dual Laterolog-Rxo Tool', *SPE 4018, Soc. Petr. Engin. 47th Ann. Conf.*, 12 pp.
- Sugimoto, Y.: 1992, 'Potential Anomaly Around Borehole in Cross-hole Resistivity Measurements – Numerical Study Using Finite Elements', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 271–279.

- Sumner, J. S.: 1976, *Principles of Induced Polarization for Geophysical Exploration*, Elsevier Sci. Publ. Co., Inc.
- Sunberg, K., Lundberg, H., and Eklund, J.: 1923, 'Electrical Prospecting in Sweden', *Sveriges Geol. Undersokning* **17**, 1–74.
- Sundberg, K. and Hedstrom, F. H.: 1934, *Structural Investigations by Electromagnetic Methods*, Proc. World Petrol. Congress **B**, part 4, 102–110, Inst. of Petroleum Technologists.
- Takacs, E.: 1993, 'In-mine Exploration of Coal Seams by the Electromagnetic Field of a Buried Vertical a.c Electric Dipole', *Annales Univ. Scient. Budapest. de Rolando Eotvos Nominatae, Sectio Geophys. et Meteorol.* **9**, 161–208.
- Thomson, S., Hatherly, P. and Liu, G.: 1990, 'The RIM in-mine Method - Theoretical and Applied studies of Its Mine Exploration Capabilities', *The Coal J.*, **29**, 33–40.
- Thomson, S. and Hind, S.: 1993, 'Bringing Geophysics into the Mine: Radio Attenuation Imaging and Mine Geology', *Explor. Geophys.* **24**, 805–810.
- Thomson, S., Young, J. and Sheard, N.: 1992, 'Base Metal Applications of the Radio Imaging Method: Current Status and Case Studies', *Expl. Geophys.*, **23**, 367–372.
- Tixier, M. P., Alger, R. P., Biggs, W. P. and Carpenter, B. N.: 1963, 'Dual Induction-laterolog: A New Tool for Resistivity Analysis', *SPE 713, Soc. Petr. Eng. Ann. Conf.*
- Torres-Verdin, C. and Habashy, T. M.: 1994, 'Rapid 2.5-Dimensional Forward Modeling and Inversion Via a New Nonlinear Scattering Approximation', *Radio Science* **29**, 1051–1079.
- Tyne, E. D., 1980, 'A review of Mise à la Masse Surveys at Elura', in D. W. Emerson (ed.), *Geophysics of the Elura Orebody, Cobar, New South Wales*, Austr. Soc. Expl. Geophys., Melbourne, pp. 186–187.
- Tyne, E. D. and Daggar, D. H.: 1990, 'Analysis of Induced Polarization and Radiometric Logs from a Test Borehole in Hawkesbury Sandstone', *Expl. Geophys.* **21**, 53–63.
- Tyne, E. D., Thorburn, M. J., and Daggar, D. H.: 1985, 'A Major Advance in Borehole IP Logging Technology', *Expl. Geophys.* **16**, 303–308.
- Uchida, T., Lee, K. H., and Wilt, M. J.: 1991, 'Effect of a Steel Casing on Crosshole EM Measurement', *61st Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 442–445.
- Unterberger, R. R.: 1978, 'Radar Propagation in Rock Salt', *Geophys. Prosp.* **26**, 312–328.
- Ushijima, K.: 1989, 'Exploration of Geothermal Reservoir by the Mise-à-la-masse Measurement', *Goetherm. Resource Counc. Bull.* **18**, 17–25.
- Ushijima, K., Mizunaga, H., Furuya, S., and Motomatsu, T., 1992, 'Fluid Flow Tomography Survey in Takigami Geothermal Field', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 247–259.
- Ushijima, K., Mizunaga, H., Tamura, Y., and Ookouchi, Y., 1992, 'Vertical Electrical Profiling Survey in Kitanigoro Area', in N. Asakura (ed.), *Geotomography*, Soc. Expl. Geophys. Japan, Tokyo, pp. 261–270.
- Vail, W. B., Momii, S. T., Woodhouse, R., Albery, M., Peveraro, R. C. A., and Klein, J. D.: 1993, 'Formation Resistivity Measurements Through Metal casing', *34th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper F, pp. 1–20.
- van Bemmelen, W.: 1908, 'Registration of Earth-currents at Batavia for the Investigation of the Connection Between Earth-current and Force of Earth-magnetism', *Kon. Akad. Van Wetens. te Amsterdam*, Part I, Proc. **10**, no. 2, 512–523; Part II, Proc. **10**(2), 782–789; Part III, Proc. **11**, 242–248.
- van Nostrand, R. G. and Cook, K. L.: 1966, *Interpretation of Resistivity Data*, U.S.G.S. Prof. Paper 499.
- Vinegar, H. J. and Waxman, M. H.: 1984, 'Induced-polarization of Shaly Sands', *Geophysics* **49**, 1267–1287.
- Vogelsang, D., Grinat, M., and Pape, H.: 1992, 'Logging of Induced Polarization in the KTB-Oberpfalz VB Interpreted by a Fractal Model', *Scientific Drilling* **3**, 105–114.
- Vozoff, K., Smith, G. H., Hatherly, P. J., and Thomson, S.: 1993, 'An Overview of the Radio Imaging Method in Australian Coal Mining', *First Break* **11**, 13–21.
- Wagg, D. M. and Seigel, H. O.: 1963, 'Induced Polarization in Drill Holes', *Can. Min. J.* **84**, 54–59.
- Wait, J. R. (ed.): 1959, *Overvoltage Research and Geophysical Applications*, Pergamon Press.
- Wait, J. R.: 1970, *Electromagnetic Waves in Stratified Media*, Pergamon Press, New York.

- Wait, J. R.: 1976, 'Note on the Transmission of Electromagnetic Waves in a Coal Seam', *Radio Science* **11**, 263–265.
- Wait, J. R.: 1989, 'Complex Resistivity in the Earth', in J. A. Kong (ed.), *Progress in Electromagnetics Research (PIER)*, Elsevier, pp. 1–173.
- Wait, J. R. and Spies, K. P.: 1972, 'Dipole Excitation of Ultralow-frequency Electromagnetic Waves in the Earth', *J. Geophys. Res.* **77**, 7118–7120.
- Ward, S. H.: 1980, 'History of Geophysical Exploration – Electrical, Electromagnetic and Magnetotelluric Methods', *Geophysics* **45**, 1659–1666.
- Ward, S. H. and Harvey, H. A.: 1954, *Electromagnetic Surveys of Diamond Drill Holes*, Can. Min. Manual, p. 19–30. Published by National Business Publications, Gardenvale, Quebec.
- Waxman, M. H. and Smits, L. J. M.: 1968, 'Electrical Conductivities in Oil-bearing Shaly Sands', *Soc. Pet. Eng. J.* **8**, 107–122.
- Webster, B., 1986, 'Time Domain IP Borehole Logging', in P. G. Killeen (ed.), *Borehole Geophysics for Mining and Geotechnical Applications*, Geol. Surv. Can. Paper 85-27, pp. 107–118.
- Wells, R. C.: 1913, 'Electrochemical Activity Between Solutions and Ores', *Econ. Geol.* **8**, 571–577.
- Wells, R. C.: 1914, 'Electric Activity in Ore Deposits', *USGS Bulletin* **548**, 78 pp.
- Wenner, F.: 1912, 'The Four-terminal Conductor and the Thomson Bridge', *U.S. Bur. Standards Bull.* **8**, 559–610.
- Wenner, F.: 1915, 'A Method of Measuring Earth Resistivity', *U.S. Bur. Standards Bull.* **12**, Sci. Paper No. 258, pp. 469–478.
- Boyd, G. W. and Wiles, C. J.: 1984, 'The Newmont Drill-hole Electromagnetic Pulse System – Examples from Eastern Australia', *Geophysics* **49**, 949–956.
- Wilt, M. and Ranganayaki, R. P.: 1990, 'Surface-to-borehole Electromagnetic Logging for Enhanced Oil Recovery (EOR) Applications', *60th Ann. Intern. Mtg., Soc. Expl. Geophys., Expanded Abstracts*, pp. 532–534.
- Wilt, M., Alumbaugh, D. L., Morrison, H. F., Becker, A., Lee, K. H. and Deszcz-Pan.: 1995, 'Crosswell Electromagnetic Tomography: System Design Considerations and Field Results', *Geophysics* **60**, 871–885.
- Winter, H., Stoll, J. and Aulbach, E.: 1991, 'The New Electrical Potential Logging Tool', *Scientific Drilling* **2**, 147–159.
- Witherly, K. E.: 1980, 'Application of Applied Potential and Downhole Pulse EM Techniques to Exploration for Massive Sulfide Deposits in E. Canada', *50th Ann. Intern. Mtg., Soc. Expl. Geophys., Reprints*, Paper M35.
- Witterholt, E. J. and Kretzschmar, J. L.: 1982, 'The Application of Crosshole Electromagnetic Wave Measurements to Mapping of a Steam Flood', *33rd Ann Mtg., Petrol. Soc. of Can. Inst. Min.*, Paper 82-33-81.
- Witterholt, E. J. and Kretzschmar, J. L.: 1984, 'Mapping of a Steam Flood with MHz EM Waves', *54th Ann. Intern. Mtg., Soc. Expl. Geophys.*, Expanded Abstracts, pp. 719–721.
- Worthington, M. H., Kuckes, A. and Oristaglio, M.: 1981, 'A Borehole Induction Procedure for Investigating Electrical Conductivity Structure Within the Broad Vicinity of a Hole', *Geophysics* **46**, 65–67.
- Wu, X. and Habashy, T. M.: 1994, 'Influence of Steel Casings on Electromagnetic Signals', *Geophysics* **59**, 378–390.
- Wyllie, M. R. J.: 1948, 'A Quantitative Analysis of the Electrochemical Component of the SP Curve', *Trans. SPE, AIME* **186**.
- Wyllie, M. R. J.: 1957, *The Fundamentals of Electric Log Interpretation*, Academic Press, New York.
- Young, J. and Rogers, G.: 1994, 'Australian Development of Tomographic Radio Imaging as a New tool in Mining Geophysics', *Buturi-Tannsa (Geophys. Explor.; Soc. Expl. Geophys. Japan)* **47**, 249–255.
- Zablocki, C. J.: 1966, 'Some Applications of Geophysical Logging Methods in Mineral Exploration Drill Holes', *7th Ann. Logging Symp. Trans.*, Soc. Prof. Well Log Anal., paper U, pp. 1–13.