

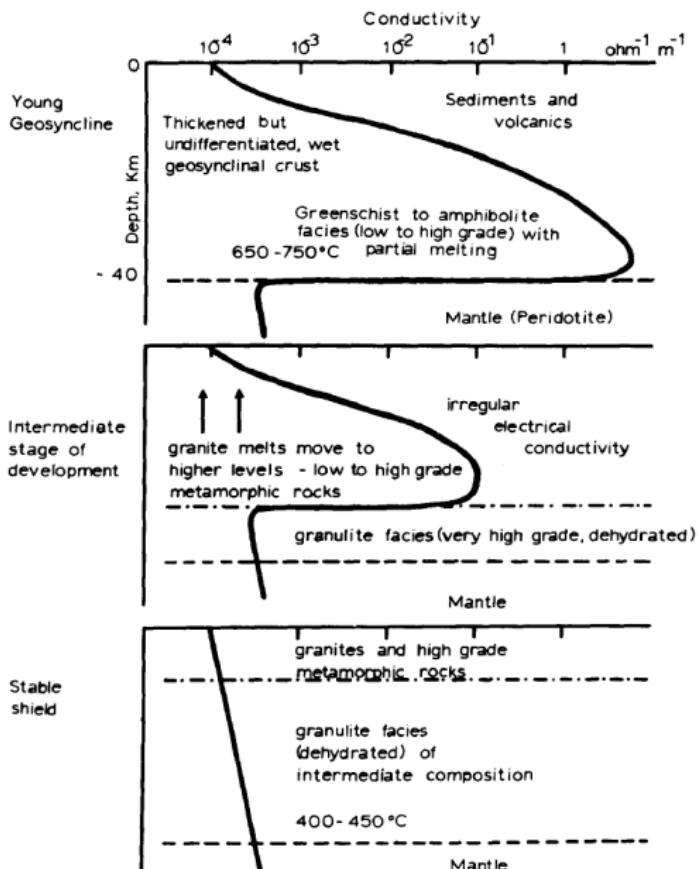
# Distinguishing melt and fluids from graphite in the lower crust with multi-physics inversion

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# The beginnings

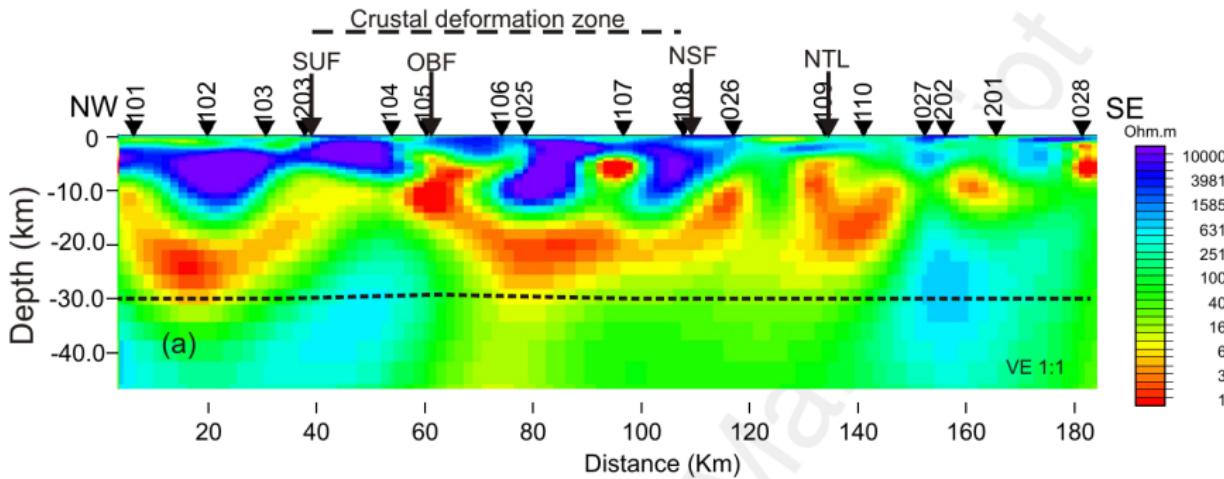


- Early EM studies (50s and 60s) inferred high conductivity in the continental crust in many areas
- First model by Hyndman and Hyndman (1968)
- Suggest fluids as a cause in "young" areas

# Historical context

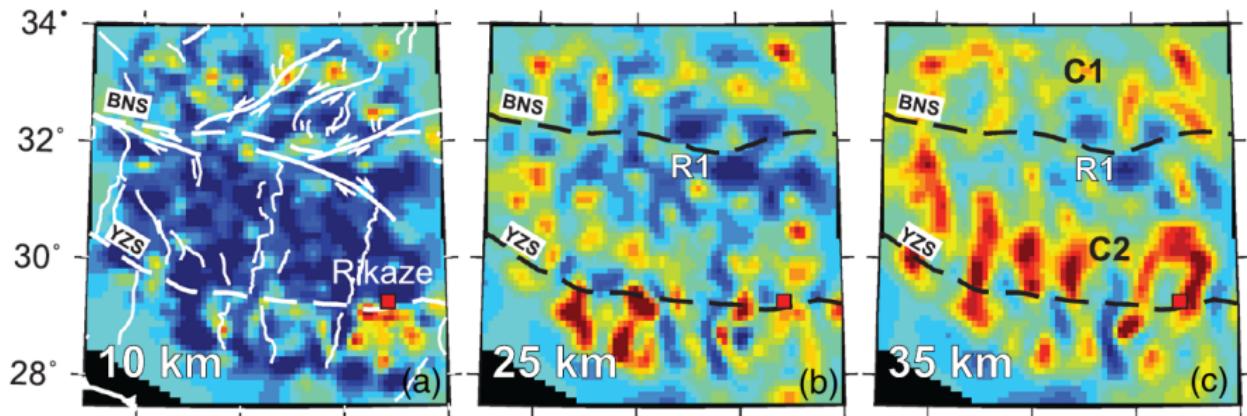
*It might be added that the only deep anomaly which could explain the anomalous variations along the coast would consist of a step in the surface of the conductive core of enormous dimensions. On the oceanic side the depth of the core could not be greater than about 20km; on the continental side the depth of the core would range between 80 and 250 km depending on the period.*

Schmucker, 1964



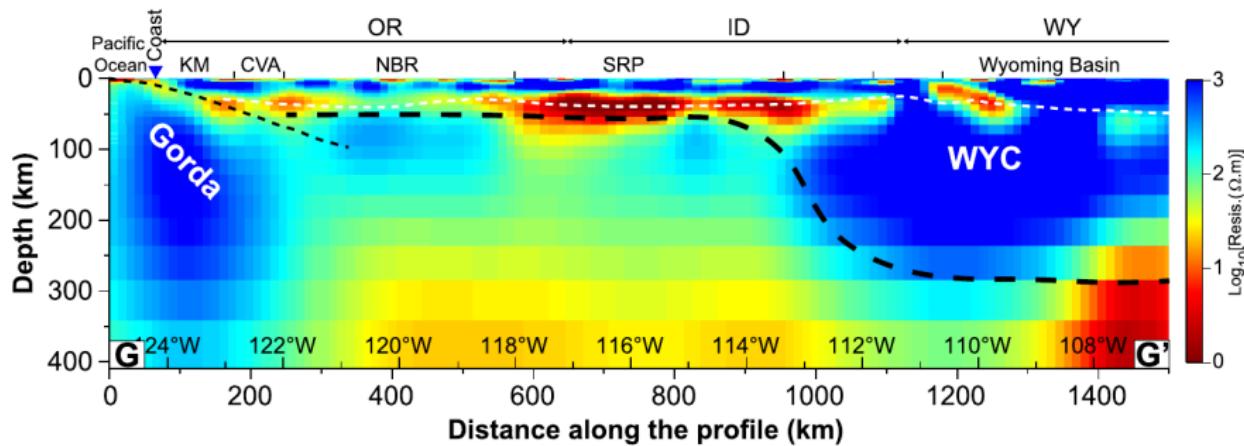
Graphite/Sulfide in metamorphosed Ordovician sediments  
Rao et al., 2007

# Tibet



Fluids/Melt associated with ongoing tectonic activity  
Dong et al., 2020

# Western United States



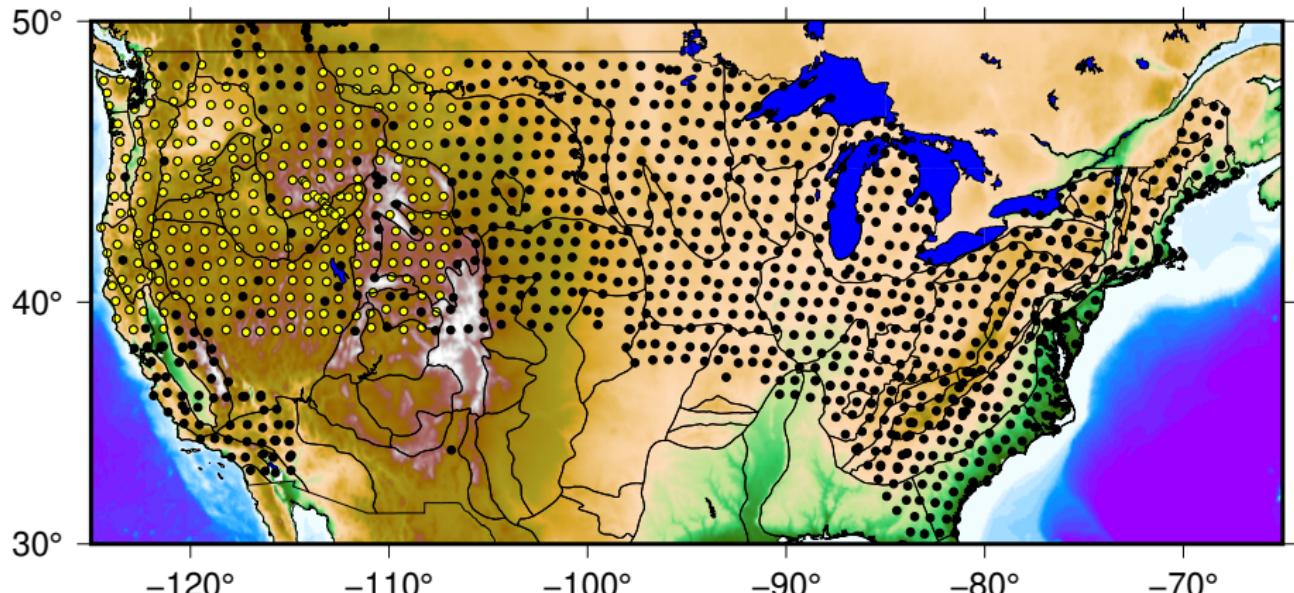
Fluids/Melt associated with ongoing tectonic activity  
Meqbel et al., 2014

# Modern explanations

Typically small amounts of connected conductive phase (1-10%) in resistive host rock

- Saline fluids, need to be retained, sometimes invoked in combination with melt (Tibet, Western US)
- Melt, needs high heat, active areas
- Graphite, remnant of past activity (fluids, deformation)
- Sulfides, less favored recently, thought to be not very abundant

# USArray – Magnetotellurics



High quality MT measurements for lithospheric imaging across continental US.  
Combine with satellite gravity data (XGM2016).

# Joint inversion

- Combine different datasets to create consistent model and improve information content.
- Here Magnetotellurics (conductivity  $\sigma$ ) and gravity (density  $\rho$ )

$$\Phi(\sigma, \rho) = \Phi_{MT}(\sigma) + \Phi_{grav}(\rho) + \Phi_{coupling}(\sigma, \rho)$$

- Minimize combination of data misfit terms  $\Phi_{MT}(\sigma)$ ,  $\Phi_{grav}(\rho)$  and coupling  $\Phi_{coupling}(\sigma, \rho)$ .
- Coupling crucial and defines expected connection.

# Mutual information (MI)

- MI measures amount of information contained in variable  $X$  about variable  $Y$  (e.g. conductivity and density)
- Definition

$$I(X, Y) = H(X) + H(Y) - H(X, Y)$$

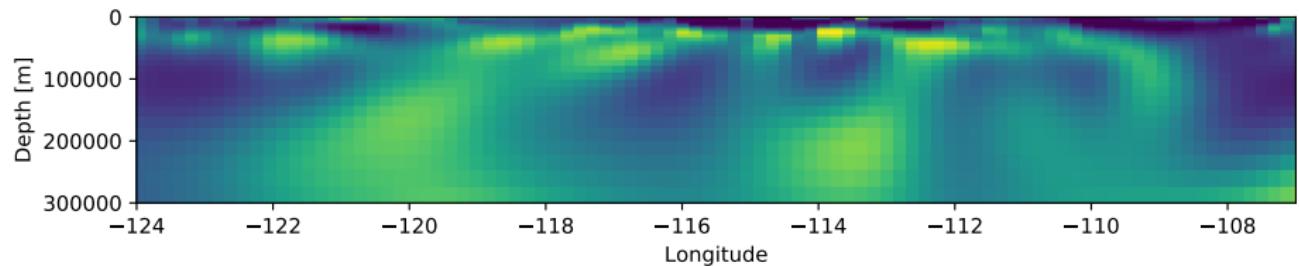
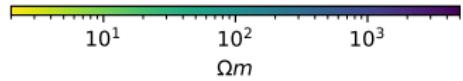
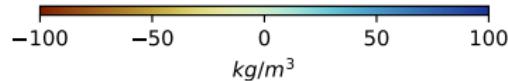
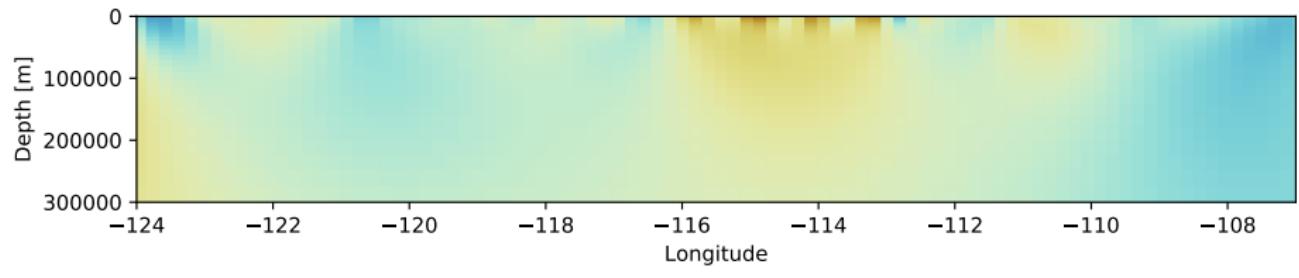
where

$$H(X) = - \sum_{i=1}^N P(x_i) \log P(x_i)$$

is the Shannon Entropy.

- Maximize mutual information as part of the inversion

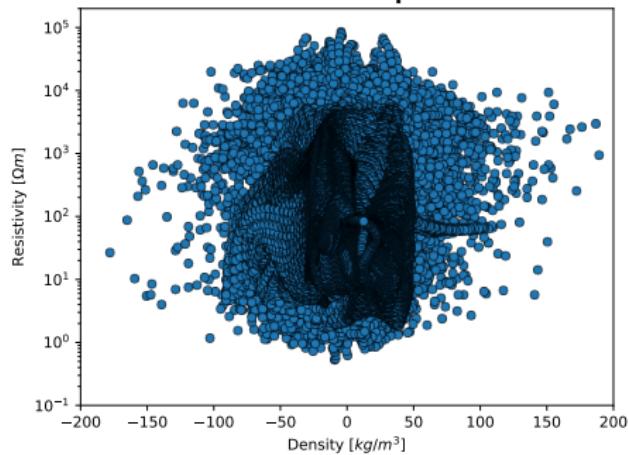
# Mutual information – illustration



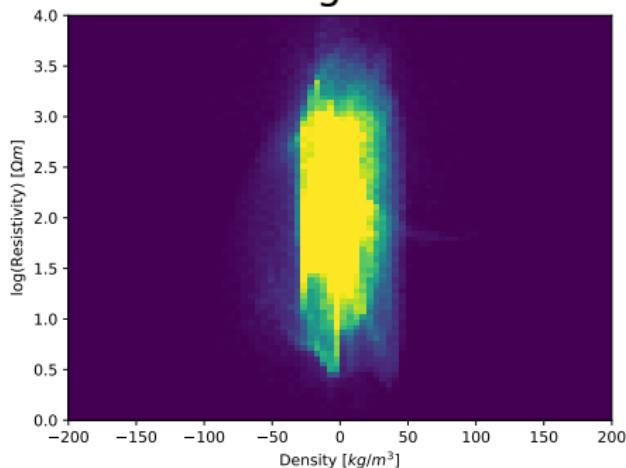
Individual models do not show similar features.

# Mutual information – illustration

Parameter plot



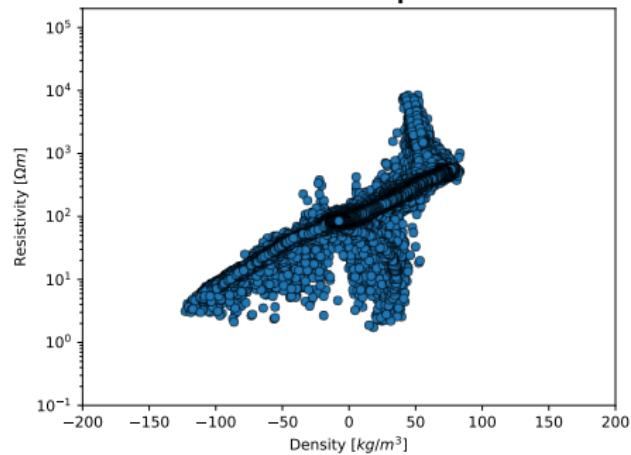
Histogram



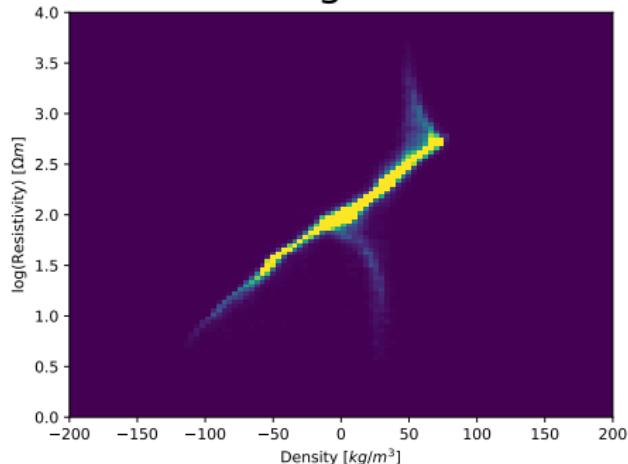
No relationship → low mutual information

# Mutual information – illustration

Parameter plot

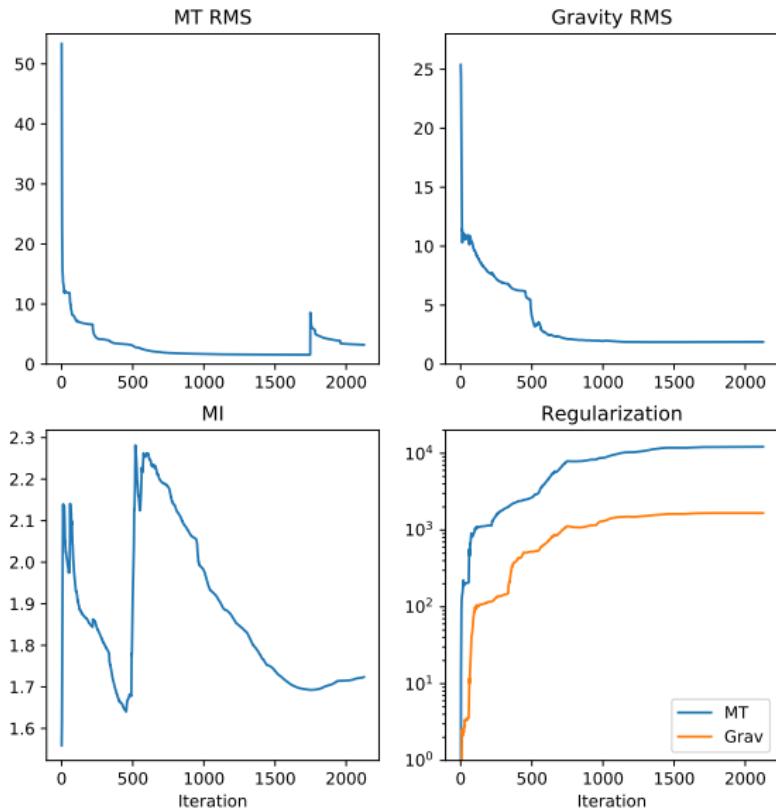


Histogram



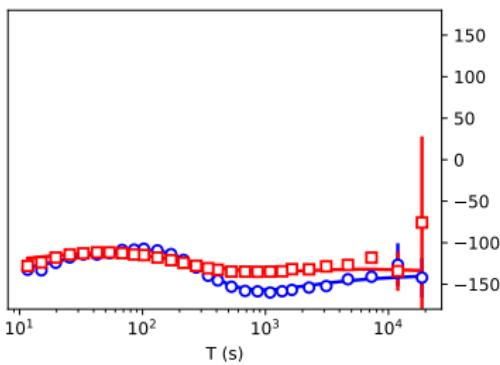
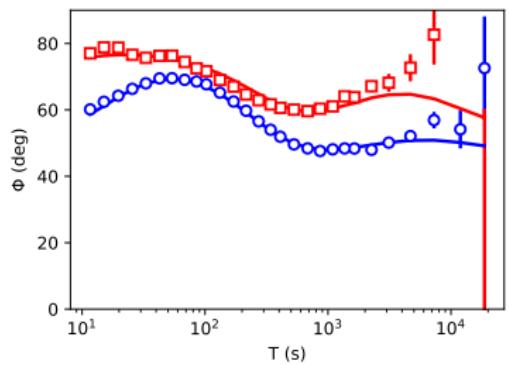
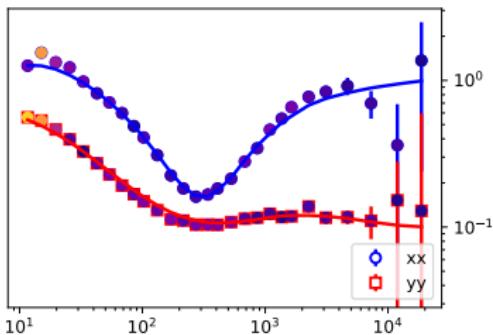
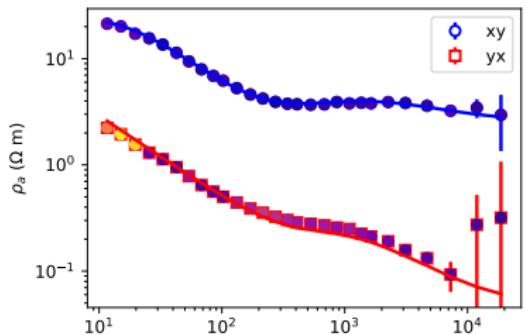
Noisy relationship → higher mutual information

# Convergence

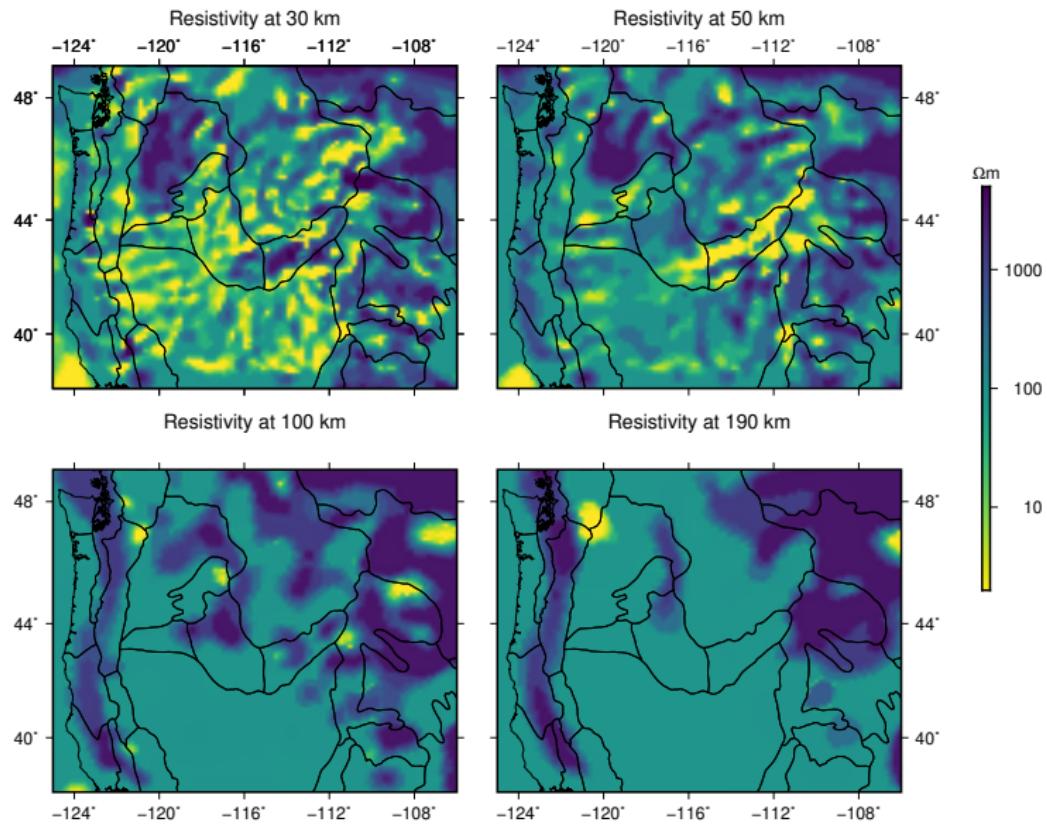


# Data fit – MT

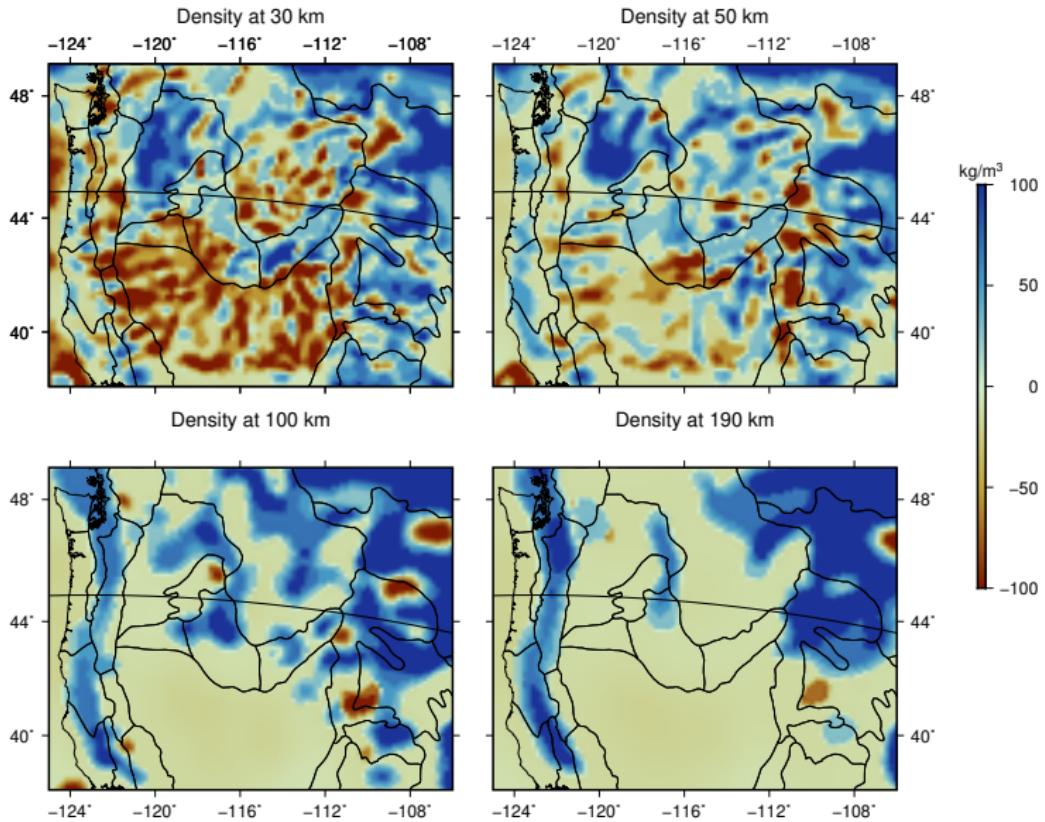
42: X 4978962.02479 Y 1259145.83622



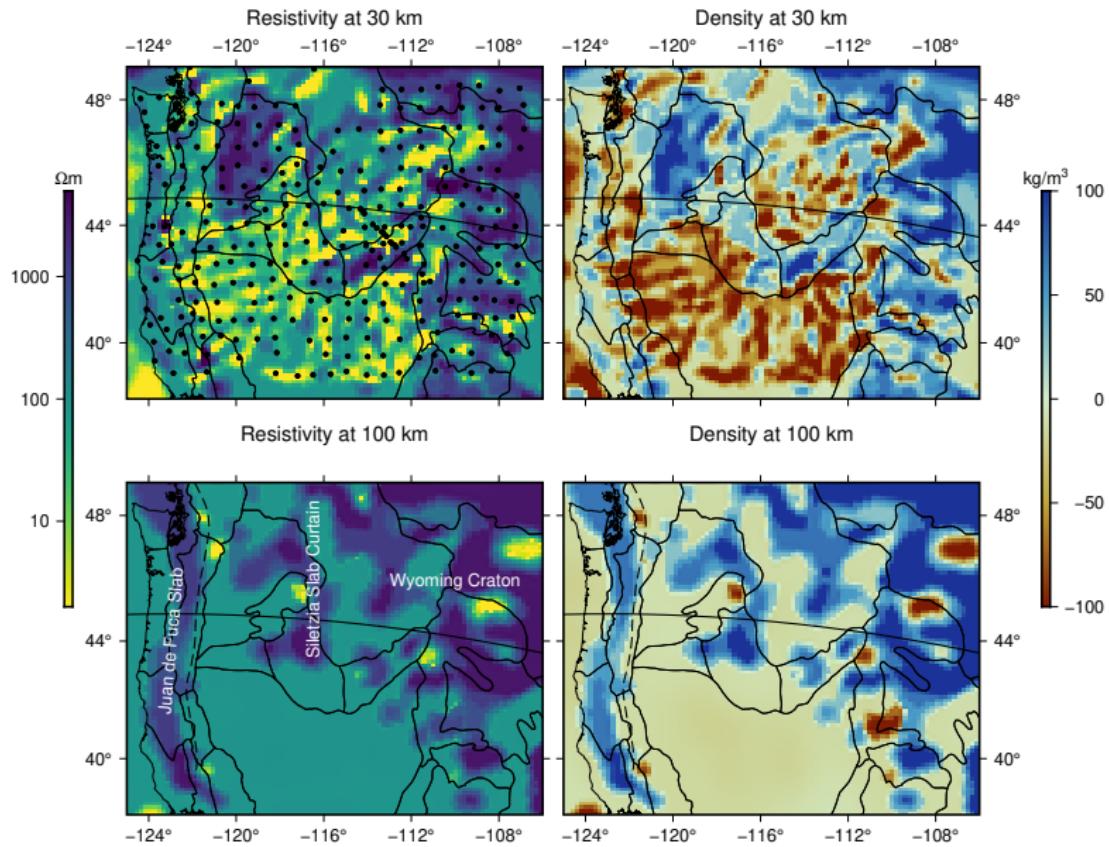
# Joint inversion with MI – resistivity



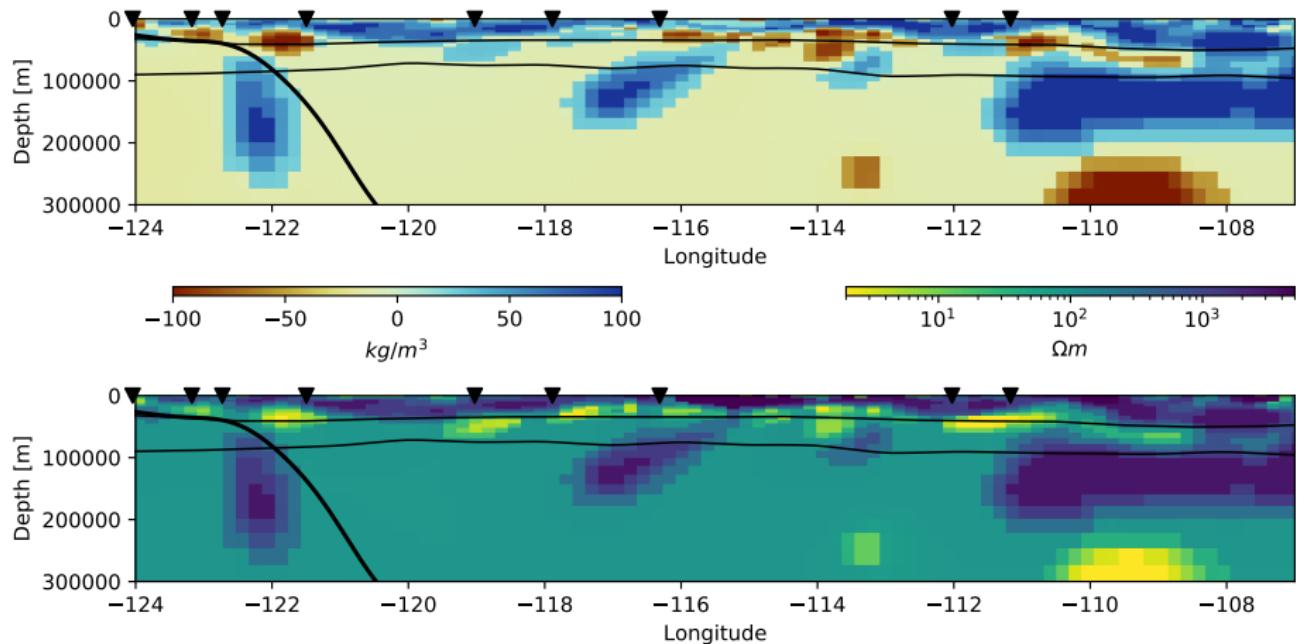
# Joint inversion with MI- density



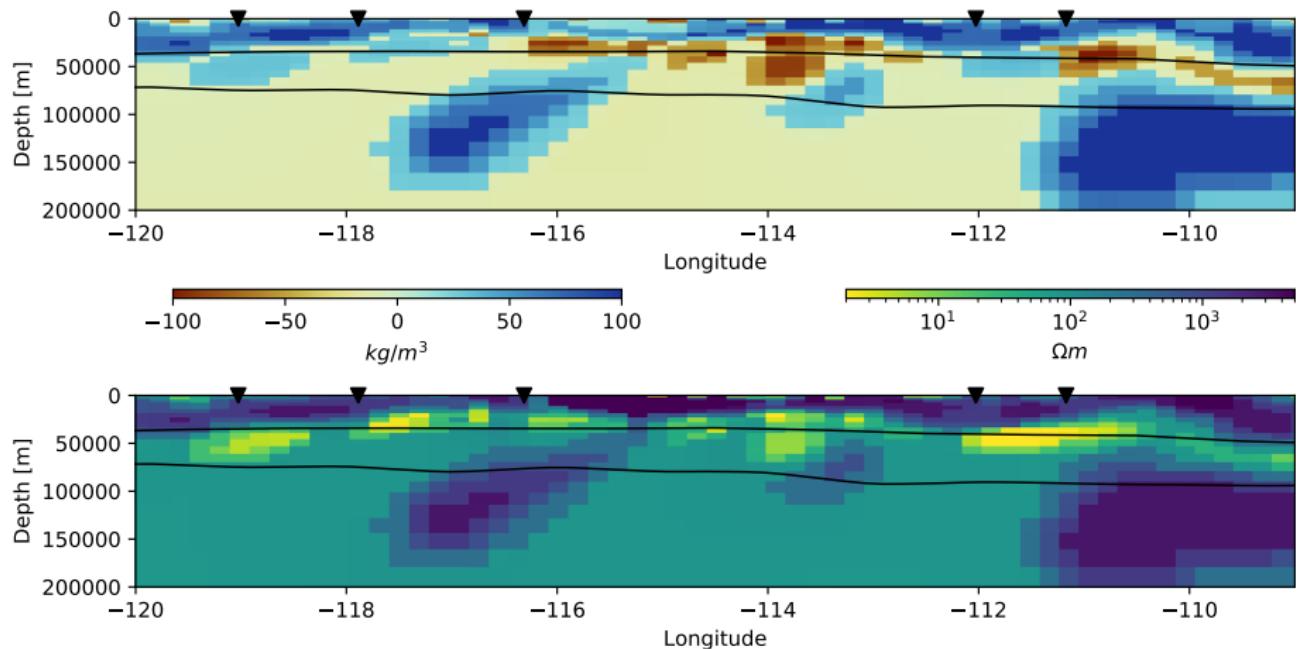
# Joint inversion with MI



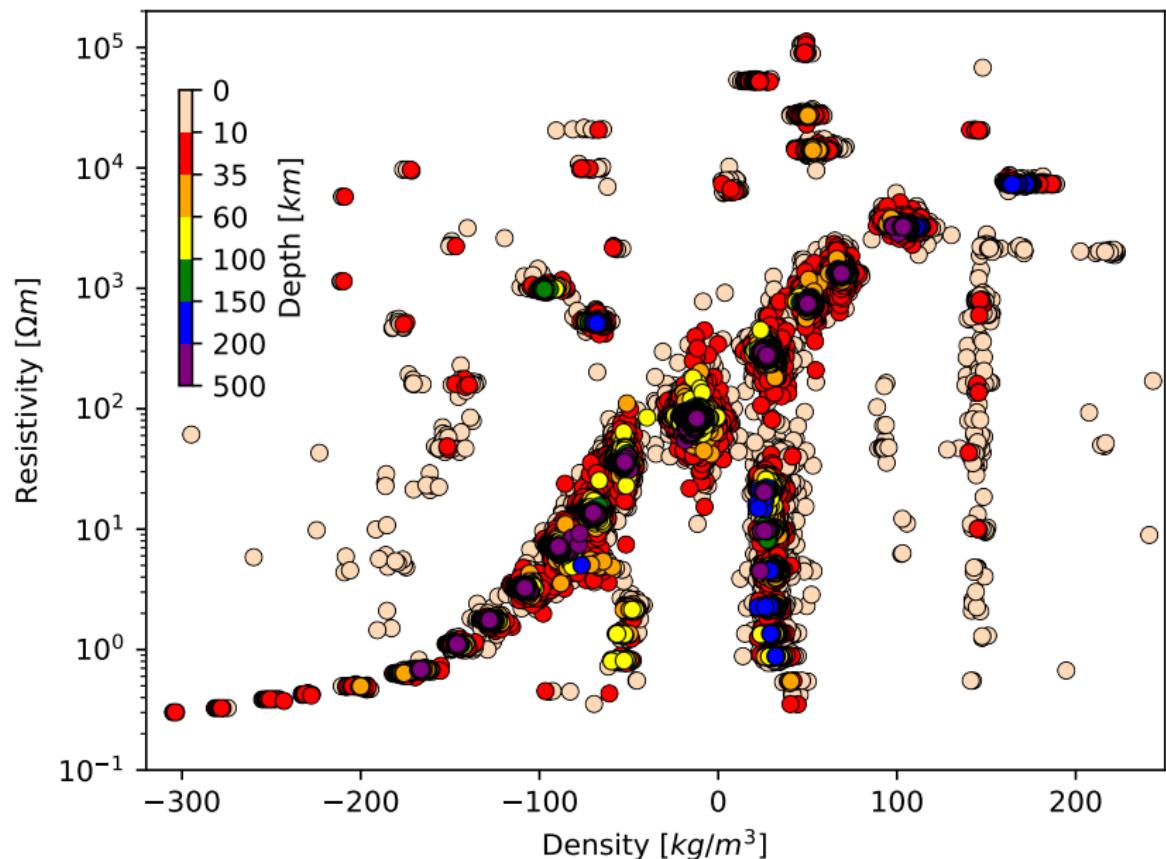
# Joint inversion with MI – vertical profile



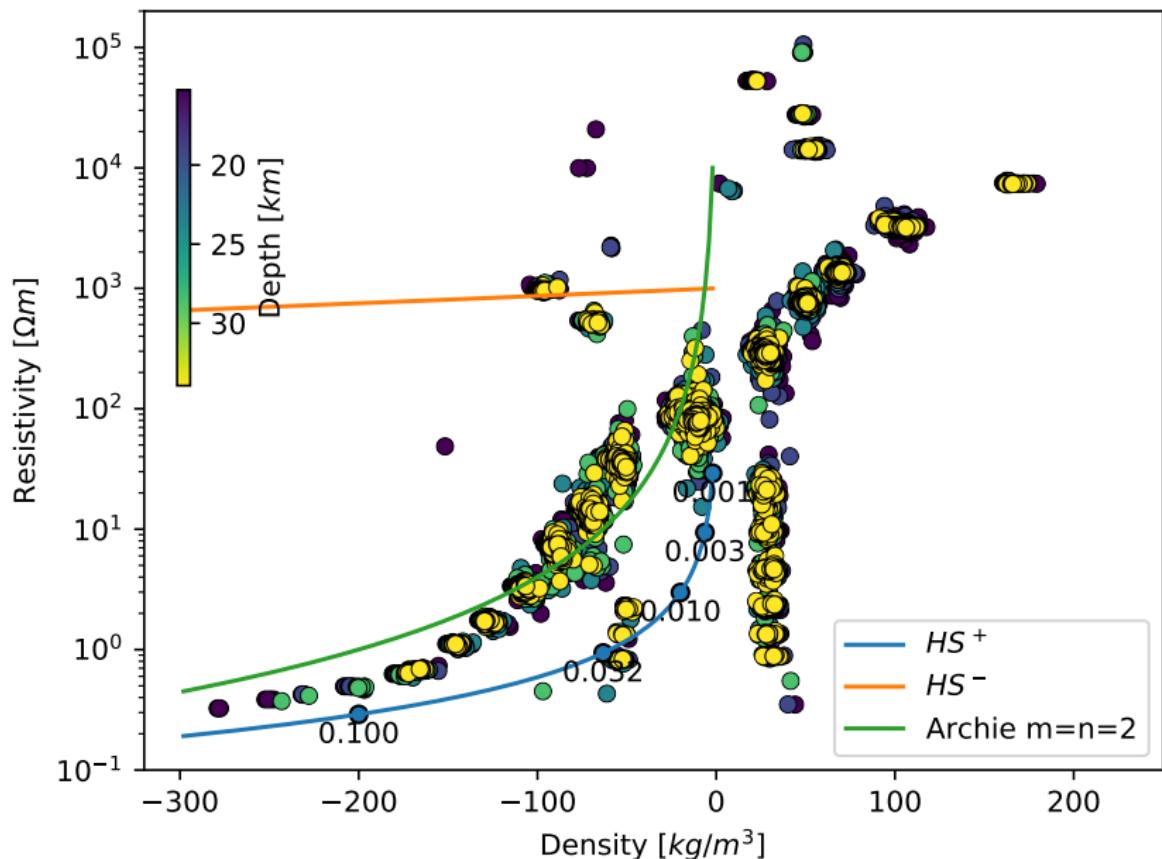
# Joint inversion with MI – vertical profile



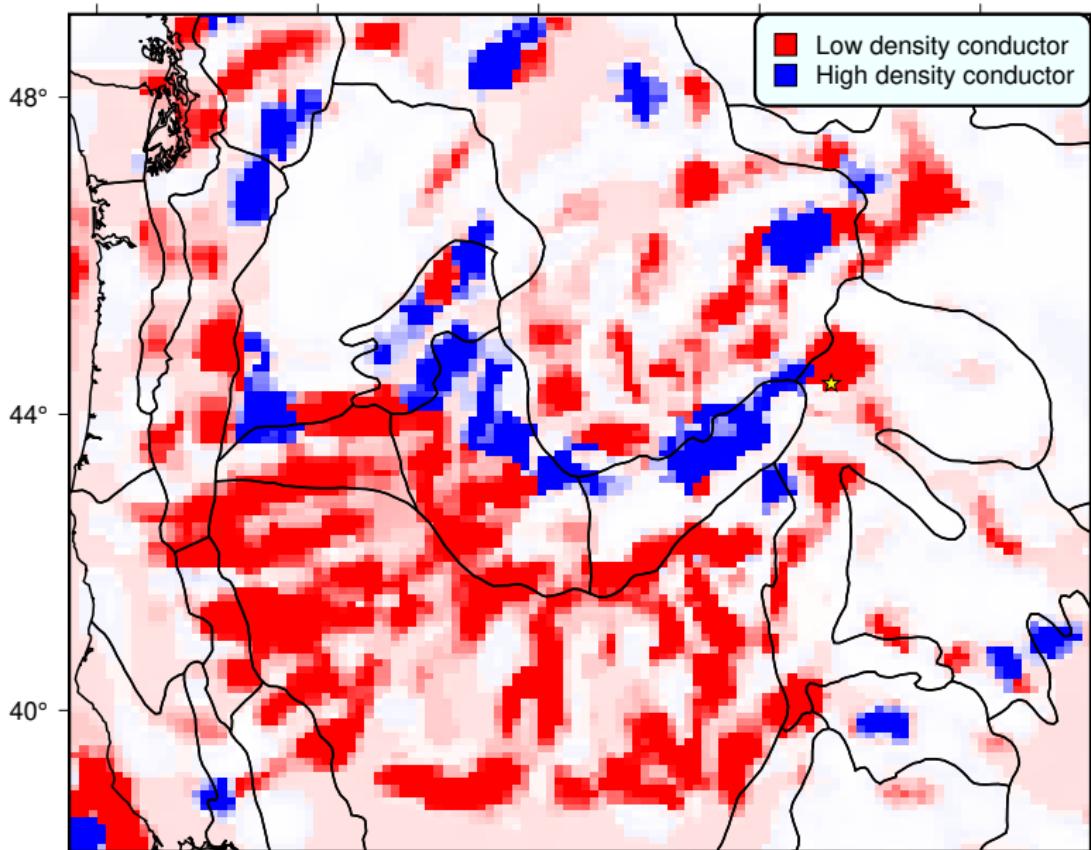
# Parameter relationship –whole model



# Parameter relationship –crust only



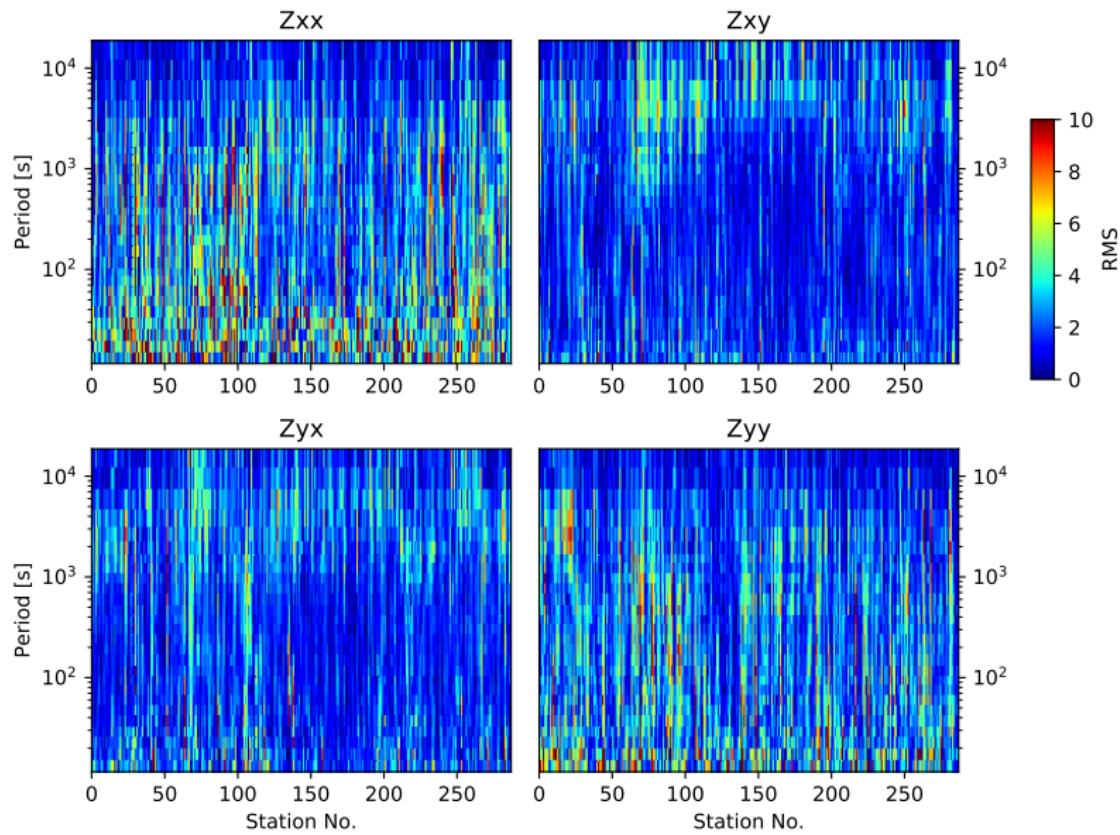
# Crustal conductors



# Conclusions

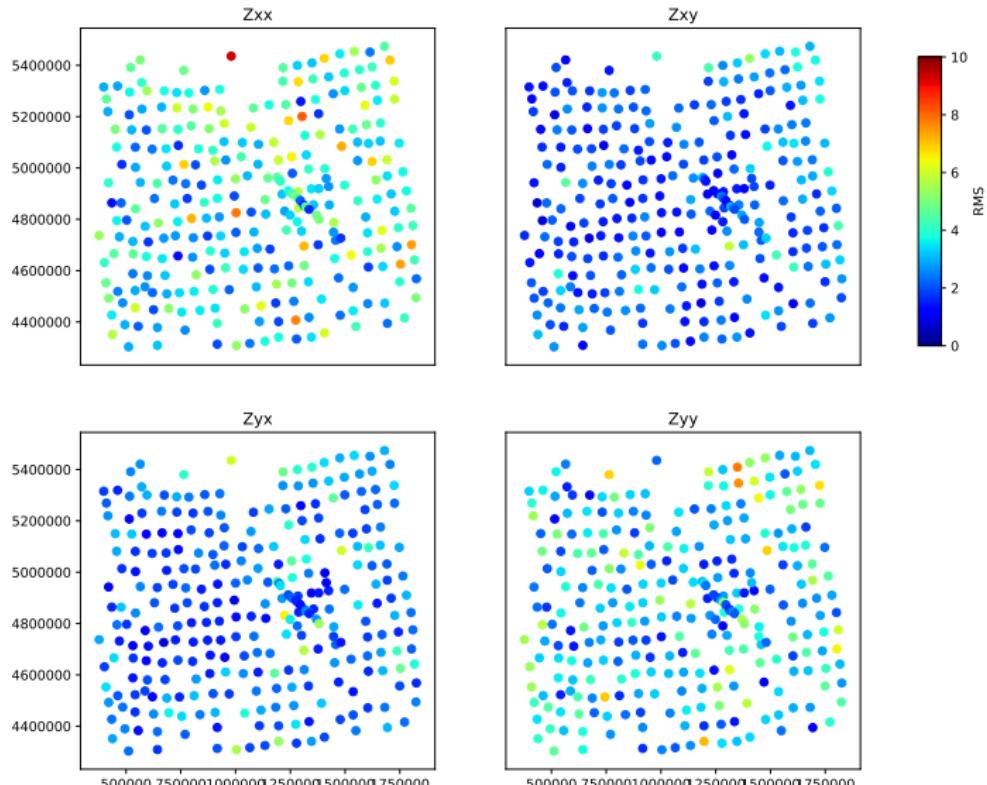
- Have developed new joint inversion with a mutual information coupling constraint
- Application to USArray data with MT and Gravity gives detailed models with many interesting features
- Retrieve well defined density-conductivity relationship, can be related to tectonic features
- Suggests current simple interpretation approaches of crustal conductivity are not tenable

# MT misfit section



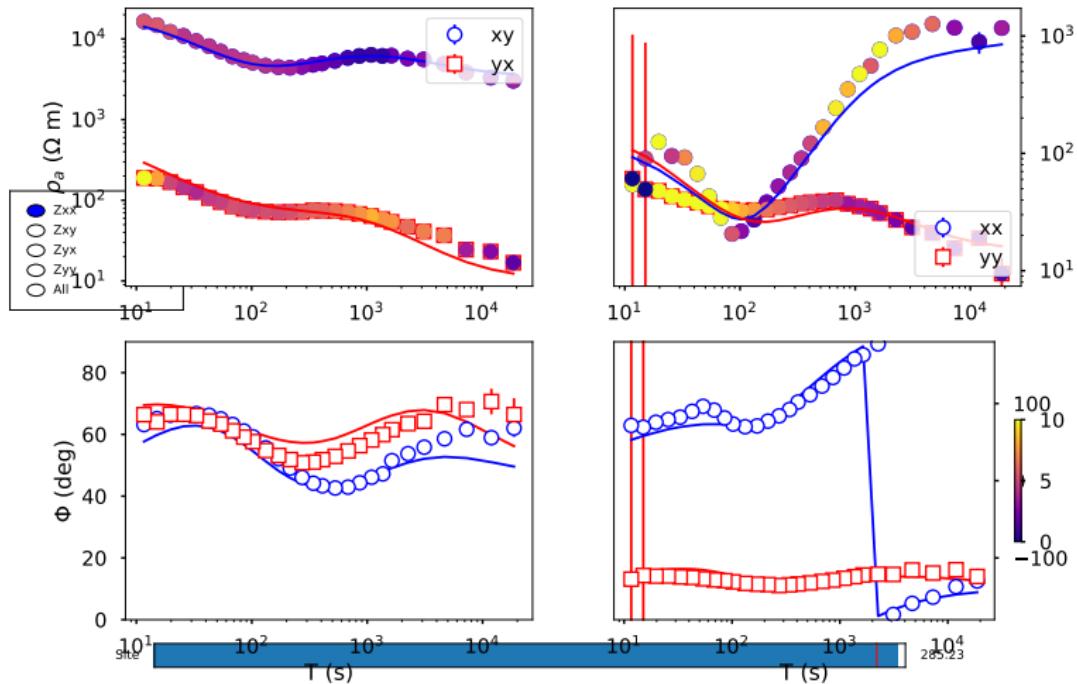
# MT misfit map

Frequency 0 - 27 : 5.340577e-05 - 0.08593753 Hz



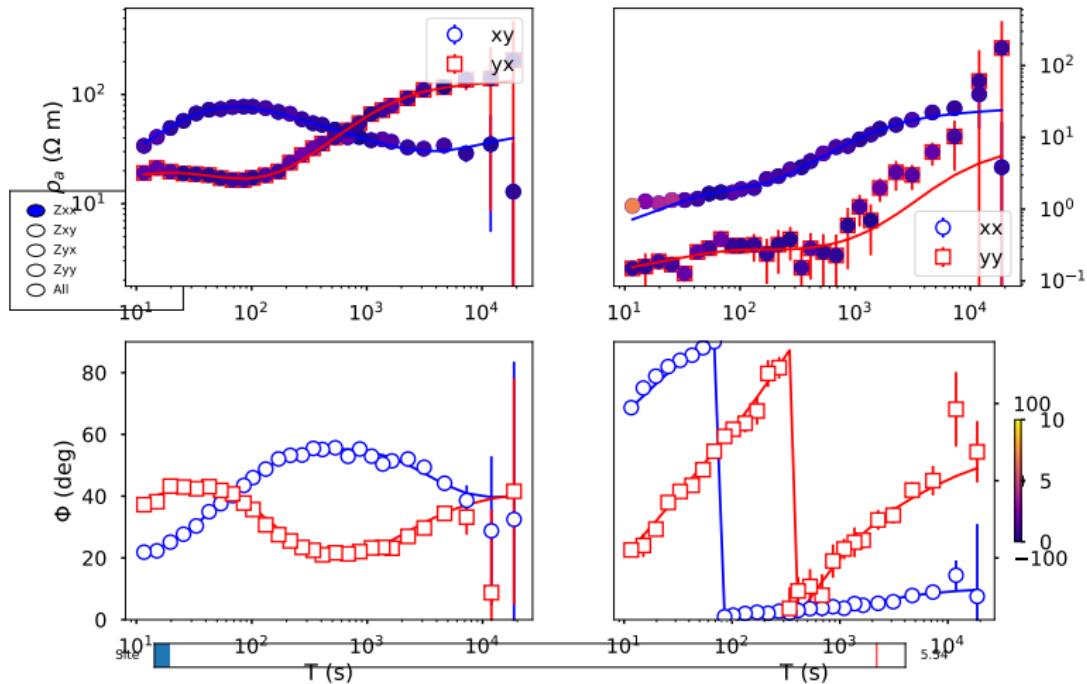
# MT worst fit

107: X 5084427.52134 Y 1484023.90588



# MT best fit

226: X 5207363.37297 Y 514732.664251



# MT misfitsection

